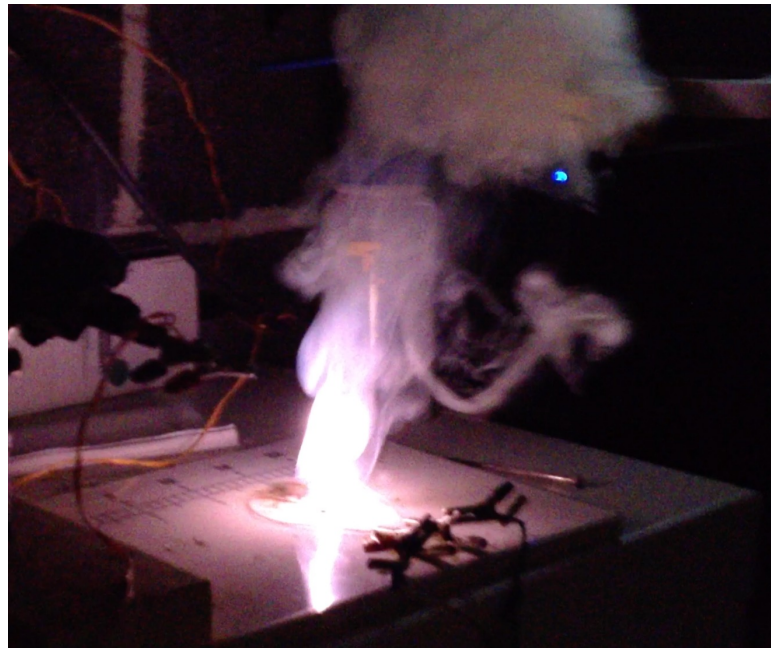


Chapter 15

Entropy and Gibbs Energy



Thermodynamics

Study of Energy Changes During Observed Processes

Δ = change

Enthalpy (H): Energy of reaction, often described in terms of heat (CHM 101)

Entropy (S): Measurement of disorder

Free Energy (G):

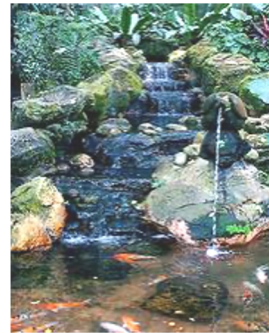
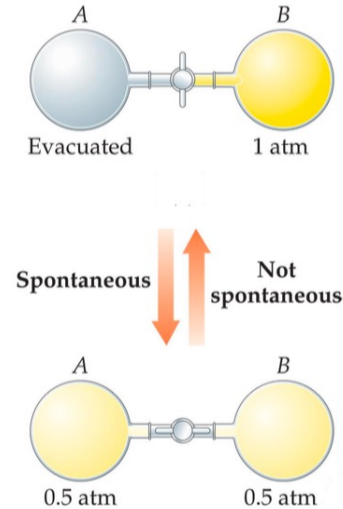
- Used to predict whether a process will occur spontaneously
- Spontaneously = without assistance
- Spontaneous process = one that will occur under a given set of conditions
- Depends on enthalpy, entropy, and temperature

$$\Delta G = \Delta H - T\Delta S$$

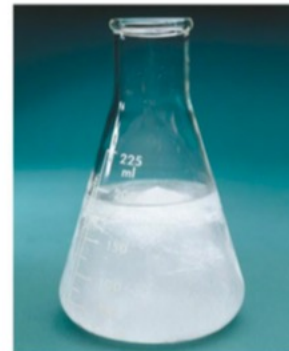


Spontaneous Processes

- Processes that are spontaneous in one direction are non-spontaneous in the other direction.
- Spontaneous processes can be fast (e.g. explosion) or slow (e.g. rusting)
- Spontaneity generally temperature dependent
 - $> 0^{\circ}\text{C}$, ice melting is spontaneous
 - $< 0^{\circ}\text{C}$, ice freezing is spontaneous

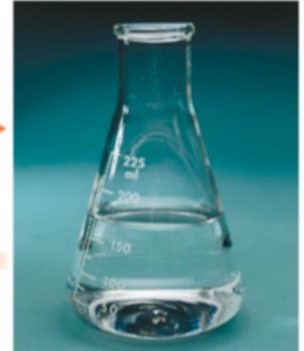


Water flows naturally downhill but must be pumped uphill



Spontaneous for $T > 0^{\circ}\text{C}$

Spontaneous for $T < 0^{\circ}\text{C}$



Spontaneous Processes

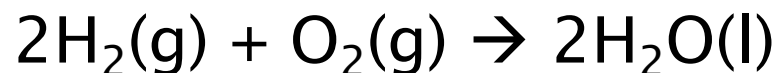
Which of the following processes are spontaneous?

- (a) Separating a mixture of N_2 and O_2 into two separate samples
- (b) Alignment of iron filings in a magnetic field
- (c) Dissolution of HCl(g) in water to form HCl(aq)
- (d) Sublimation of $\text{CO}_2(\text{s})$ at -100°C , 1 atm (CO_2 sublimation point is -78°C , 1 atm)
- (e) Reaction of copper with oxygen to form CuO under typical environmental conditions in RI.

Enthalpy & Spontaneity

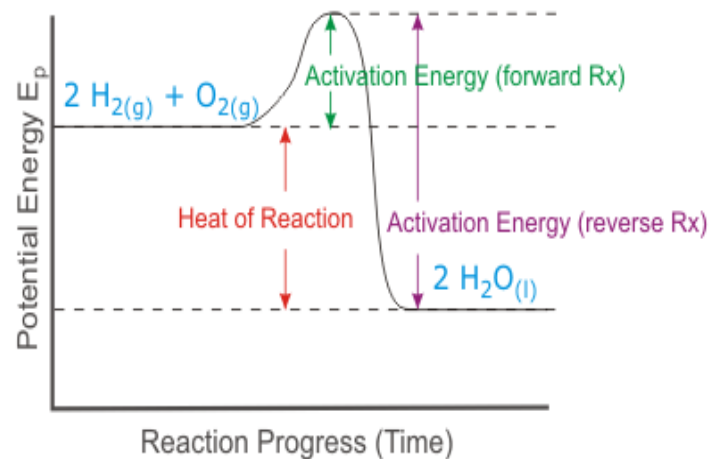
Reaction of H_2 & O_2 to form H_2O

- Used in fuel cells
- Exothermic reaction
- $\Delta H = -286 \text{ kJ/mol}$
- Favors H_2O production



Reality at room temp:

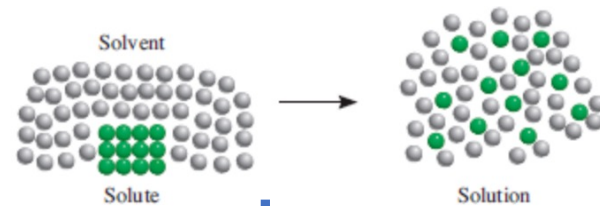
- Not a spontaneous reaction
- H_2 & O_2 remain unreacted
- No water is formed without added energy to initiate
- $E_{\text{act}} = +112 \text{ kJ/mol}$ – too high



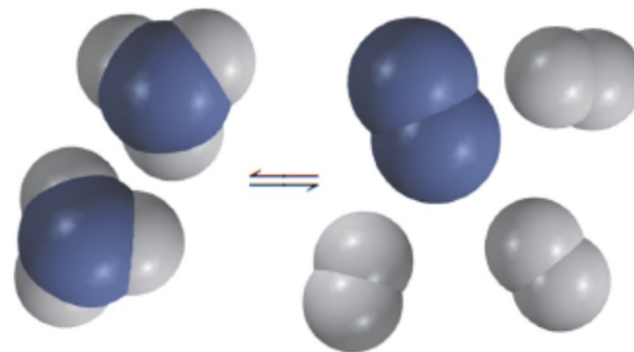
Enthalpy determines the equilibrium state, but enthalpy alone does NOT determine spontaneity
Also need to consider entropy

Entropy (S)

Entropy is defined as a measure of the randomness or disorder of a system, or how spread out a system's energy is



- It is related to the various modes of motion in molecules (or of ions/atoms)
- Entropy is a state function (like enthalpy & total energy)
 - State functions are defined by final-initial conditions (independent of process)
 - $\Delta S = S_{\text{final}} - S_{\text{initial}}$
- Entropy is increased when, for example:
 - Moles of products > moles of reactants
 - More complex molecules are broken down into smaller, simpler molecules
 - There is a phase change to a more disordered phase (disorder: gas>liquid>solid)



Entropy & Microstates

Entropy is related to the number of “microstates” through the equation:

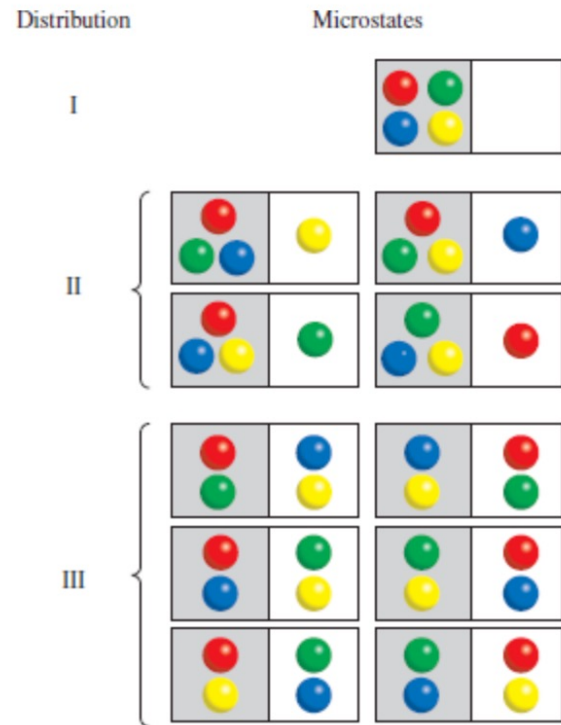
$$S = k \ln W$$

k = Boltzmann constant (1.38×10^{-23} J/K)

W = # microstates.

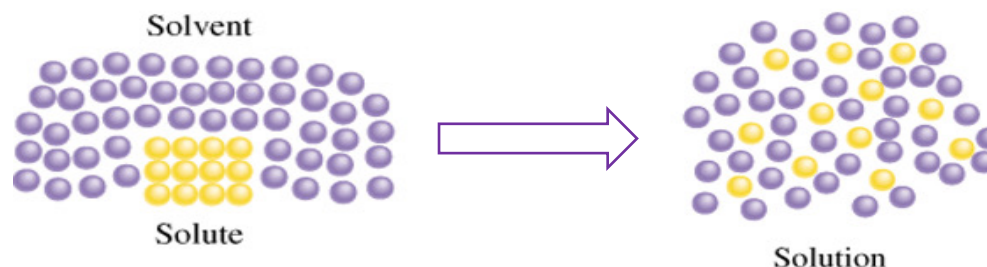
$$\begin{aligned}\Delta S &= S_f - S_i \\ &= k \ln W_f - k \ln W_i \\ &= k \ln (W_f/W_i)\end{aligned}$$

Microstate is a term used to describe the number of ways that a given state can be achieved.



More possible variation = More microstates = Higher S

Entropy & Solvation



Generally, dissolving a solute in a solvent increases entropy

However:

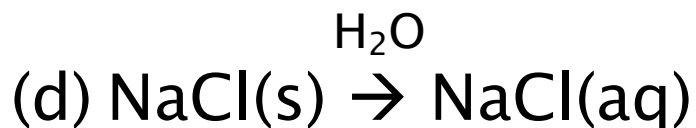
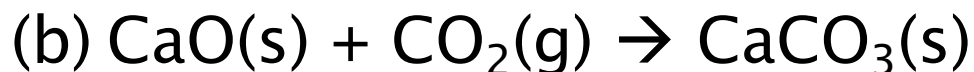
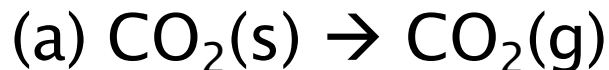
When solutes are dissolved, the water molecules around them have less ability to move due to interactions with the solute (H-bonds, ion-dipole interactions, etc.).

In some cases (especially with large ions or those with large charges) this results in an overall decrease in entropy.

| Dissolution Equation | $\Delta S_{\text{soin}}^{\circ}$ (J/k · mol) |
|--------------------------------------------------------------------------------------|----------------------------------------------|
| $\text{NH}_4\text{NO}_3 (s) \rightarrow \text{NH}_4^{+} (aq) + \text{NO}_3^{-} (aq)$ | 108.1 |
| $\text{AlCl}_3 (s) \rightarrow \text{Al}^{3+} (aq) + 3\text{Cl}^{-} (aq)$ | -253.2 |
| $\text{FeCl}_3 (s) \rightarrow \text{Fe}^{3+} (aq) + 3\text{Cl}^{-} (aq)$ | -266.1 |

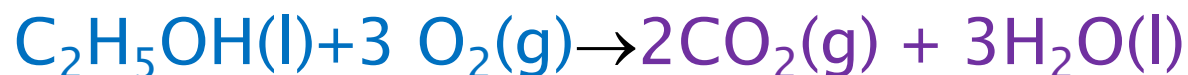
Predicting Entropy Changes

Indicate whether the following produces an increase or decrease in the entropy of the system:



CHM 101 Review: Calculating Reaction Enthalpy from Standard Enthalpies of Formation

$$\Delta H_{\text{reaction}} = \Sigma \Delta H_{\text{products}} - \Sigma \Delta H_{\text{reactants}} \quad (\Sigma = \text{sum})$$



- **ΔH_f° Reactants:**

- $\text{C}_2\text{H}_5\text{OH}(\text{l})$: $-277.7 \text{ kJ/mol} \times 1 = -277.7 \text{ kJ/mol}$
- O_2 : $0.0 \text{ kJ/mol} \times 3 = 0.0 \text{ kJ/mol}$
- Total reactants = $-277.7 \text{ kJ/mol} + 0.0 \text{ kJ/mol} = -277.7 \text{ kJ/mol}$

- **ΔH_f° Products**

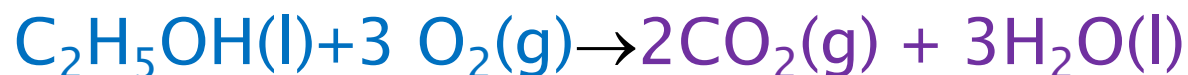
- $\text{CO}_2(\text{g})$: $-393.5 \text{ kJ/mol} \times 2 = -787.0 \text{ kJ/mol}$
- $\text{H}_2\text{O}(\text{l})$: $-285.8 \text{ kJ/mol} \times 3 = -857.4 \text{ kJ/mol}$
- Total products = $-787.0 \text{ kJ/mol} + -857.4 \text{ kJ/mol} = -1644.4 \text{ kJ/mol}$

- $\Delta H^\circ = \Sigma \Delta H_{\text{products}} - \Sigma \Delta H_{\text{reactants}}$

$$= -1644.4 \text{ kJ/mol} - (-277.7 \text{ kJ/mol}) = -1366.7 \text{ kJ/mol}$$

Calculating Reaction Entropy from Standard Entropies

$$\Delta S_{\text{reaction}} = \Sigma S^{\circ}_{\text{products}} - \Sigma S^{\circ}_{\text{reactants}} \quad (\Sigma = \text{sum})$$



S° Reactants:

- $\text{C}_2\text{H}_5\text{OH}(\text{l})$: $161.2 \text{ J/mol K} \times 1 = 161.2 \text{ J/mol K}$
- O_2 : $205.0 \text{ J/mol K} \times 3 = 615.0 \text{ J/mol K}$
- Total reactants = $161.2 \text{ J/mol K} + 615.0 \text{ J/mol K} = 776.2 \text{ J/mol K}$

S° Products

- $\text{CO}_2(\text{g})$: $213.6 \text{ J/mol K} \times 2 = 427.2 \text{ J/mol K}$
- $\text{H}_2\text{O}(\text{l})$: $69.9 \text{ J/mol K} \times 3 = 209.7 \text{ J/mol K}$
- Total products = $427.2 \text{ J/mol K} + 209.7 \text{ J/mol K} = 636.9 \text{ J/mol K}$

$$\begin{aligned} \Delta S^{\circ} &= \Sigma S_{\text{products}} - \Sigma S_{\text{reactants}} \\ &= 636.9 \text{ J/mol K} - 776.2 \text{ J/mol K} = -139.3 \text{ J/mol K} \end{aligned}$$

Some Standard Molar Entropy Values (larger table in Appendix 2 of Textbook)

TABLE 15.2

Standard Entropy Values (S°) for Some Substances at 25°C

| Substance | S° (J/K · mol) | Substance | S° (J/K · mol) |
|----------------------|-----------------------|--------------------|-----------------------|
| H ₂ O (l) | 69.9 | C(diamond) | 2.4 |
| H ₂ O (g) | 188.7 | C(graphite) | 5.69 |
| Na (s) | 51.05 | O ₂ (g) | 205.0 |
| Na (l) | 57.56 | O ₃ (g) | 237.6 |
| Na (g) | 153.7 | F ₂ (g) | 203.34 |
| He (g) | 126.1 | Au (s) | 47.7 |
| Ne (g) | 146.2 | Hg (l) | 77.4 |

$$S^\circ_{\text{gas}} > S^\circ_{\text{liquid}} > S^\circ_{\text{solid}}$$

For similar molecules, S° tends to increase with:

- Increasing molar mass
- Increased number of atoms in formula

Standard Molar Entropies of Selected Substances at 298 K

| Substance | S° , J/mol-K |
|-----------|---------------------|
|-----------|---------------------|

Gases

| | |
|---------------------|-------|
| H ₂ (g) | 130.6 |
| N ₂ (g) | 191.5 |
| O ₂ (g) | 205.0 |
| H ₂ O(g) | 188.8 |
| NH ₃ (g) | 192.5 |

Liquids

| | |
|-----------------------------------|-------|
| H ₂ O(l) | 69.9 |
| CH ₃ OH(l) | 126.8 |
| C ₆ H ₆ (l) | 172.8 |

Solids

| | |
|-----------------------|-------|
| Li(s) | 29.1 |
| Na(s) | 51.4 |
| K(s) | 64.7 |
| Fe(s) | 27.23 |
| FeCl ₃ (s) | 142.3 |
| NaCl(s) | 72.3 |

Some Enthalpies of Formation at 25°C

| Substance | ΔH_f° , kJ/mol |
|-----------------------------------|-----------------------------|
| HCl(g) | -92.31 |
| HF(g) | -271.1 |
| HI(g) | 26.48 |
| H ₂ O(g) | -241.8 |
| H ₂ O(l) | -285.8 |
| NH ₃ (g) | -46.11 |
| NO(g) | 90.25 |
| N ₂ O(g) | 82.05 |
| NO ₂ (g) | 33.18 |
| N ₂ O ₄ (g) | 9.16 |
| SO ₂ (g) | -296.8 |
| SO ₃ (g) | -395.7 |

| Ion | ΔH_f° , kJ/mol |
|-------------------------------|-----------------------------|
| H ⁺ | 0 |
| Na ⁺ | -240.1 |
| K ⁺ | -252.4 |
| NH ₄ ⁺ | -132.5 |
| Ag ⁺ | +105.6 |
| Mg ²⁺ | -466.9 |
| Ca ²⁺ | -542.8 |
| Ba ²⁺ | -537.6 |
| OH ⁻ | -230.0 |
| Cl ⁻ | -167.2 |
| NO ₃ ⁻ | -205.0 |
| CO ₃ ²⁻ | -677.1 |
| SO ₄ ²⁻ | -909.3 |

All ΔH_f are for standard conditions

25°C, 1 atm, 1M aqueous solution, 1 mole product

Enthalpy values will be needed for Gibbs Energy Calcs.

Calculating Reaction Entropy from Standard Entropies

1. What is the molar change in entropy for water freezing at 25°C? **A: -28.9 J/mol K**
2. What is the standard entropy change for the following reaction? **A: 180.0 J/K**



From table of standard entropies (J/mol K):

$S^\circ \text{H}_2\text{O}(\text{s}): 41.1$

$S^\circ \text{H}_2\text{O}(\text{l}): 70.0$

$S^\circ \text{H}_2\text{O}(\text{g}): 188.8$

$S^\circ \text{Al}_2\text{O}_3(\text{s}): 50.9$

$S^\circ \text{H}_2(\text{g}): 130.7$

$S^\circ \text{Al}(\text{s}): 28.3$

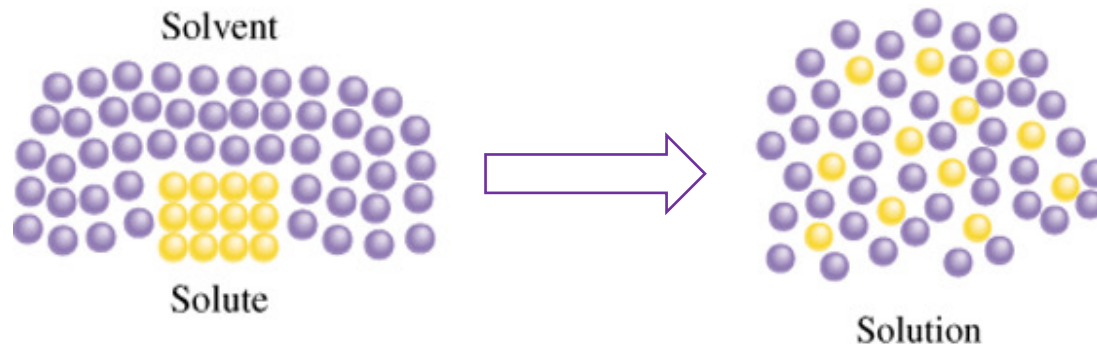
Three Laws of Thermodynamics

First Law of Thermodynamics:

- Energy cannot be created or destroyed
- The total energy of the Universe must be constant
- Energy can be converted from one form to another, or transferred between systems & surroundings

Second Law of Thermodynamics:

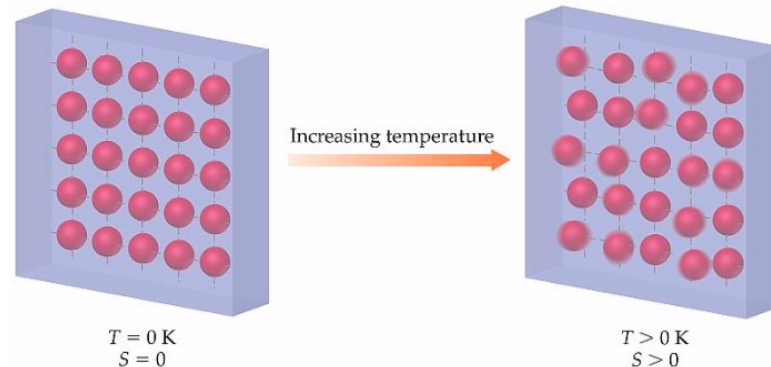
- The entropy of the Universe ($\Delta S_{\text{univ}} = \Delta S_{\text{sys}} + \Delta S_{\text{surr}}$) increases for spontaneous processes
- For spontaneous (irreversible) processes: $\Delta S_{\text{univ}} > 0$
- For reversible processes: $\Delta S_{\text{univ}} = 0$



Three Laws of Thermodynamics

Third Law of Thermodynamics:

- The entropy of a pure crystalline substance at absolute zero (0K) is zero.
- Scientists have come close to absolute zero, but 0K has not yet been achieved
- At 0K there is absolutely no molecular movement
- Provides a starting point for determining ΔS
 - Start as close to 0K as possible, warm material up to a specific temperature and calculate ΔH
 - $S = \Delta H/T$
 - Note: Since S is temp. dependent, to use this equation the process must be isothermal.

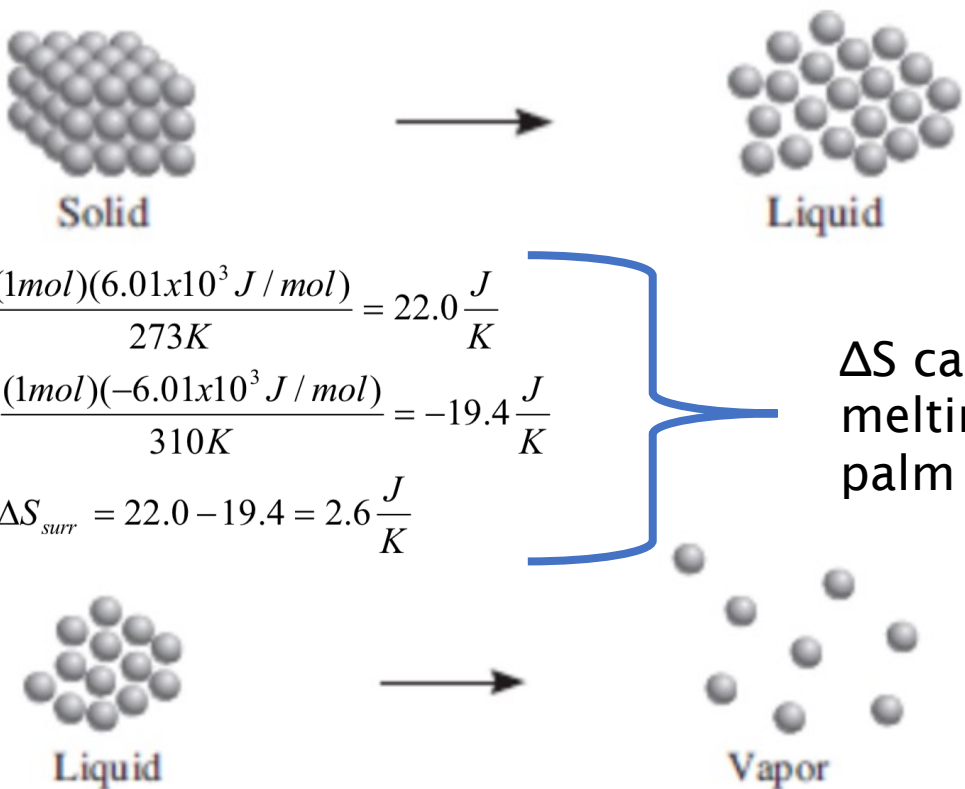


Calculating Entropy (S) from ΔH

The normal boiling point of ethanol ($\text{C}_2\text{H}_5\text{OH}$, 46.07g/mol) is 78.3°C and its molar enthalpy of vaporization is 38.56 kJ/mol. What is the change in entropy in the system when 68.3g of gaseous ethanol at 1 atm condenses to liquid at the normal boiling point? A: -163 J/K

Phase Changes & Entropy

Less Order = Greater Entropy



Solid

Liquid

Liquid

Vapor

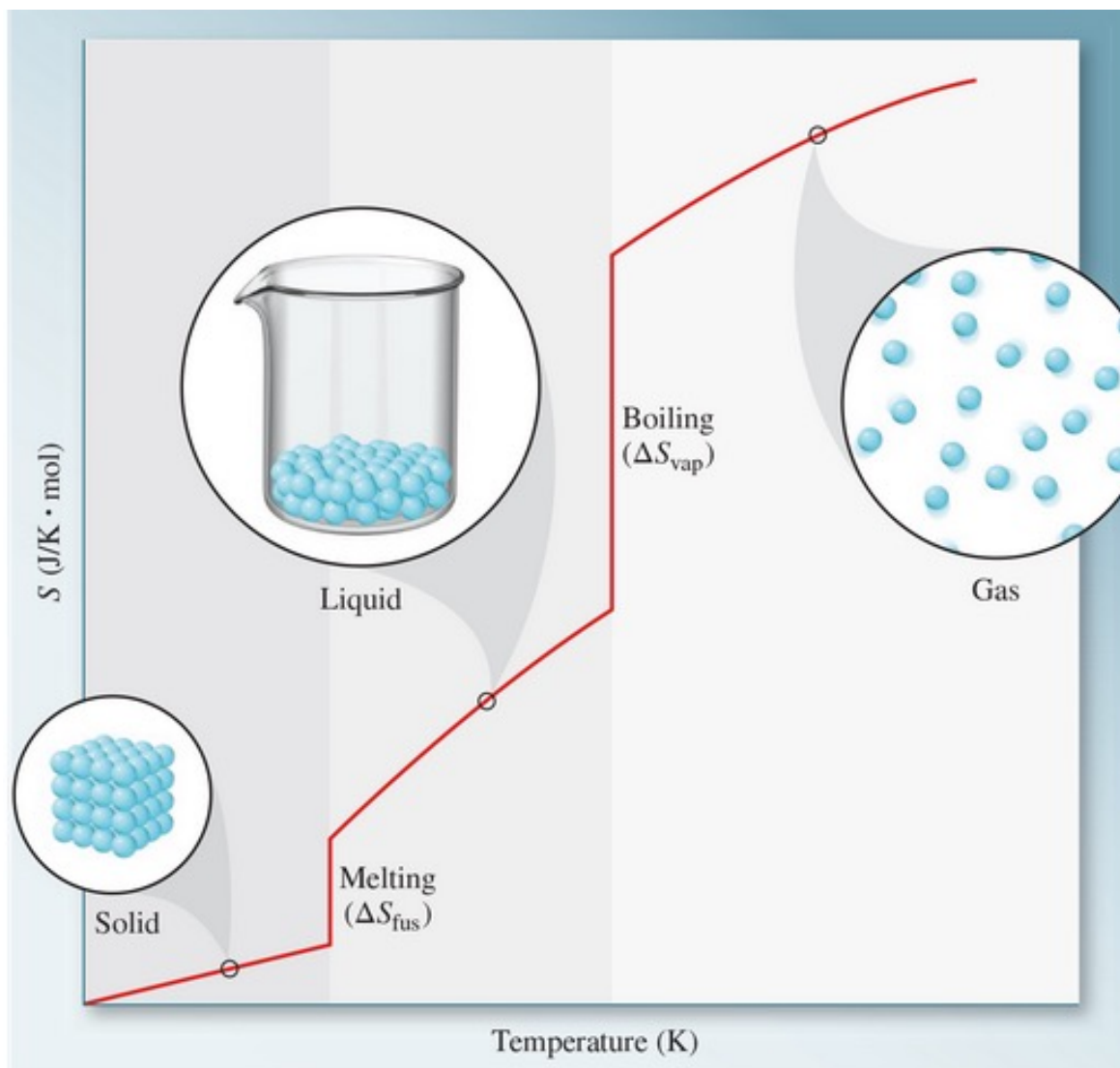
$$\Delta S_{sys} = \frac{q_{rev}}{T} = \frac{(1mol)(6.01 \times 10^3 J/mol)}{273K} = 22.0 \frac{J}{K}$$
$$\Delta S_{surr} = \frac{q_{rev}}{T} = \frac{(1mol)(-6.01 \times 10^3 J/mol)}{310K} = -19.4 \frac{J}{K}$$
$$\Delta S_{total} = \Delta S_{sys} + \Delta S_{surr} = 22.0 - 19.4 = 2.6 \frac{J}{K}$$

ΔS calculation for melting ice in the palm of your hand

Melting & Vaporization are favored by entropy

Freezing & Condensation (exothermic) are favored by enthalpy

What determines which process will occur?



Spontaneity is Temperature Dependent!

Gibbs Free Energy (G)

The maximum useful work that can be done by a system on its surroundings in a spontaneous process at constant T & P.

$$\Delta G = \Delta H - T\Delta S$$

The equation comes from thermodynamic principles

$$\text{Eq1: } \Delta S^\circ_{\text{univ}} = S^\circ_{\text{surr}} + S^\circ_{\text{sys}}$$

$$\text{Eq2: } \Delta S_{\text{surr}} = -\Delta H_{\text{sys}}/T$$

Substitute Eq2 for S°_{surr}

$$\Delta S^\circ_{\text{univ}} = (-\Delta H_{\text{sys}}/T) + S^\circ_{\text{sys}}$$

Multiply by $-T$ to get

$$-T\Delta S^\circ_{\text{univ}} = \Delta H_{\text{sys}} - T\Delta S_{\text{sys}}$$

Let $-T\Delta S^\circ_{\text{univ}} = \Delta G$ to get

$$\Delta G = \Delta H - T\Delta S$$

Standard Free Energy, ΔG°

Free energy change when reactants and products are
in their standard states

(pure material, 1 atm, 1 M if in solution,
zero for elements in standard state)

$$\Delta G^\circ_{\text{reaction}} = \sum G^\circ_{\text{f products}} - \sum G^\circ_{\text{f reactants}}$$

Gibbs Free Energy & Spontaneity

$\Delta G < 0$ (negative), the process is spontaneous

$\Delta G > 0$ (positive), the process is non-spontaneous

$\Delta G = 0$ the process is at equilibrium

| ΔH | ΔS | ΔG | Spontaneous? |
|------------|------------|------------|----------------|
| negative | positive | negative | yes |
| positive | negative | positive | no |
| negative | negative | ? | Temp Dependent |
| positive | positive | ? | Temp Dependent |

Gibbs Free Energy & Spontaneity

TABLE 15.4

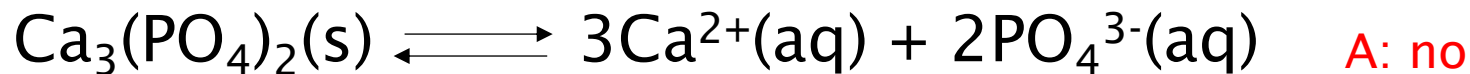
Predicting the Sign of ΔG Using  Equation 15.10 and the Signs of ΔH and ΔS

| When ΔH Is | And ΔS Is | ΔG Will Be | And the Process Is | Example |
|--------------------|-------------------|--------------------------------------|----------------------------|--------------------------------------------------------------------------------|
| Negative | Positive | Negative | Always spontaneous | $2\text{H}_2\text{O}_2(aq) \rightarrow 2\text{H}_2\text{O}(l) + \text{O}_2(g)$ |
| Positive | Negative | Positive | Always nonspontaneous | $3\text{O}_2(g) \rightarrow 2\text{O}_3(g)$ |
| Negative | Negative | Negative when $T\Delta S < \Delta H$ | Spontaneous at low T | $\text{H}_2\text{O}(l) \rightarrow \text{H}_2\text{O}(s)$ |
| | | Positive when $T\Delta S > \Delta H$ | Nonspontaneous at high T | (freezing of water) |
| Positive | Positive | Negative when $T\Delta S > \Delta H$ | Spontaneous at high T | $2\text{HgO}(s) \rightarrow 2\text{Hg}(l) + \text{O}_2(g)$ |
| | | Positive when $T\Delta S < \Delta H$ | Nonspontaneous at low T | |

Gibbs Free Energy & Spontaneity

1. A certain reaction has $\Delta H^\circ = -19.5\text{kJ}$ and $\Delta S^\circ = 42.7\text{J/K}$.
- (a) Is the reaction exothermic or endothermic? A: exothermic
- (b) Does the reaction lead to an increase or decrease in the randomness or disorder of the system? A: increase
- (c) Calculate ΔG° at 298K A: -32.2kJ
- (d) Is the reaction spontaneous at 298K under standard conditions? A: yes

2. Is the following process spontaneous at 25°C? at 75°C?



Step 1: Calculate ΔH°

From table of standard enthalpies (H°) (kJ/mol):

$\text{Ca}_3(\text{PO}_4)_2(\text{s})$: -4121

$\text{Ca}^{2+}(\text{aq})$: -542.8

$\text{PO}_4^{3-}(\text{aq})$: -1277.4

Step 2: Calculate ΔS°

From table of standard entropies (S°) (J/mol K):

$\text{Ca}_3(\text{PO}_4)_2(\text{s})$: +236

$\text{Ca}^{2+}(\text{aq})$: -53.1

$\text{PO}_4^{3-}(\text{aq})$: -220.5

Step 3: Calculate ΔG°

3. At what temperature will the following process become spontaneous?



A: -198.8°C