

Chapter 18

Acid – Base Equilibria & Solubility Equilibria



Common-Ion Effect

The extent of ionization of a weak electrolyte is decreased by the addition of a strong electrolyte that has an ion in common with the weak electrolyte.

Equilibrium process – presence of ions shifts process back to reactants.

Ex: A solution is made with 1.0M HF and 2.0M NaF



Add extra F^- from NaF

Shift equilibrium

Will affect pH if solution is acidic or basic
– in this case shift toward reactants
decreases concentration of H_3O^+ in solution.

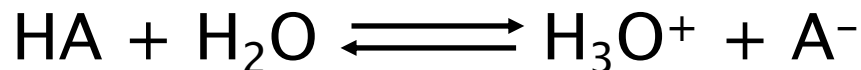
Common-Ion pH Calculations

1. Calculate the pH of a solution containing 0.085M nitrous acid (HNO_2 ; $K_a = 4.5 \times 10^{-4}$) and 0.10M potassium nitrite (KNO_2).

Buffer Solutions (Buffers)

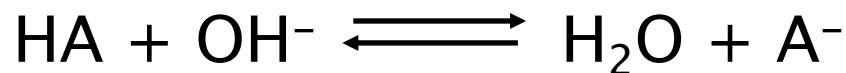
Solutions that resist changes in pH when small amounts of acid or base are added

- Must contain a weak acid or base **and**
- The conjugate (salt) of the weak acid or base
- i.e. Contain a weak conjugate acid/base pair
- pH is controlled by equilibrium [K_a (or K_b)]

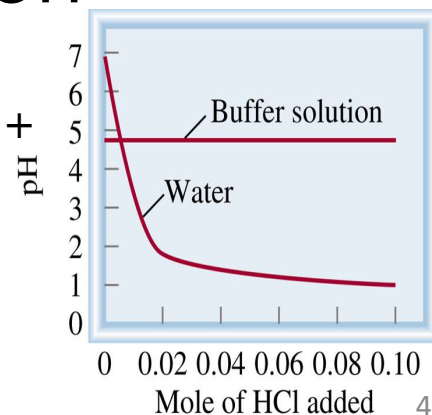
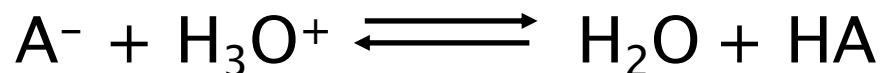


When small amounts of a strong acid or base are added:

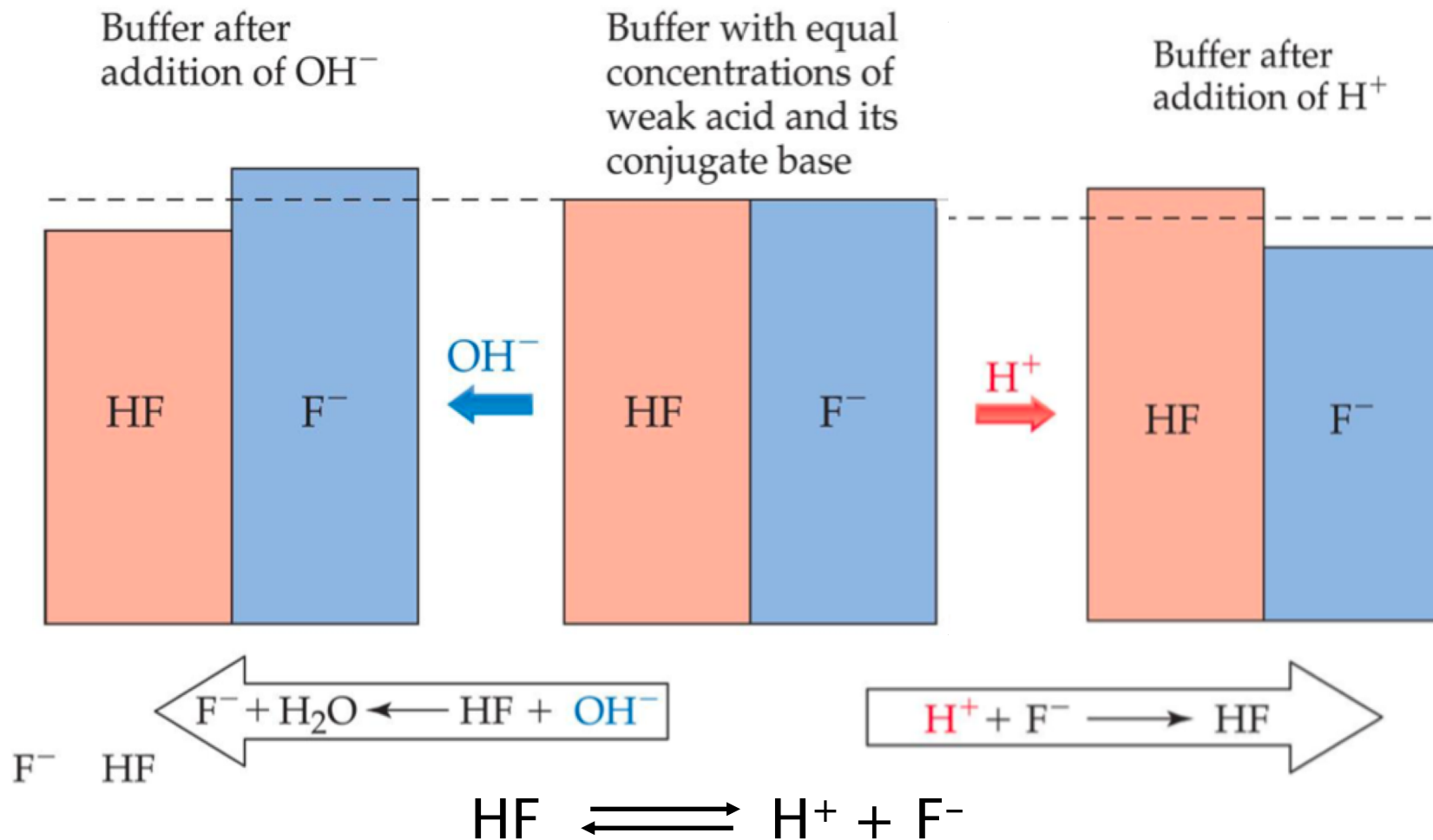
- Acidic species in buffer neutralizes added OH^-



- Basic species in buffer neutralizes added H^+



How Buffers Work – Le Châtelier's Principle



- Add OH^- , reduce H^+ , shift equilibrium toward conj. Base
 - OH^- will react with H^+ to form water
- Add H^+ , shift equilibrium toward undissociated acid

Henderson-Hasselbalch Equation

$$\text{pH} = \text{pK}_a + \log \frac{[\text{A}^-]}{[\text{HA}]}$$

Comes from the equilibrium expression for: $\text{HA} \rightleftharpoons \text{H}^+ + \text{A}^-$

$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} \implies K_a = [\text{H}^+] \frac{[\text{A}^-]}{[\text{HA}]}$$

Take the $-\log$ of both sides:

$$-\log K_a = -\log [\text{H}^+] + -\log \frac{[\text{A}^-]}{[\text{HA}]}$$

pK_a points to $-\log K_a$
 pH points to $-\log [\text{H}^+]$
Conj. base points to $[\text{A}^-]$
acid points to $[\text{HA}]$

Therefore:

$$\text{pK}_a = \text{pH} + -\log \frac{[\text{A}^-]}{[\text{HA}]}$$

For bases:

$$\text{pOH} = \text{pK}_b + -\log \frac{[\text{BH}^+]}{[\text{B}]}$$

Rearrange to get Henderson-Hasselbalch

Buffer Calculations

1. A 1.00L buffer solution is prepared that contains 0.150M nitrous acid and 0.200M sodium nitrite. What is its pH?

$$K_a = 7.2 \times 10^{-4}$$

Ice Table Method

Buffer Calculations

1. A 1.00L buffer solution is prepared that contains 0.150M nitrous acid and 0.200M sodium nitrite. What is its pH?

$$K_a = 7.2 \times 10^{-4}$$

H-H equation method:

$$\text{pH} = 3.27$$

Buffer Calculations

2. How many grams of sodium lactate ($\text{CH}_3\text{CH}(\text{OH})\text{COONa}$) should be added to 1.0L of a 0.150M lactic acid ($\text{CH}_3\text{CH}(\text{OH})\text{COOH}$) to form a buffer solution with $\text{pH}=4.00$?
 $K_a = 1.4 \times 10^{-4}$; molar mass of sodium lactate = 112.1g/mol

Buffer Capacity

Buffer Capacity: The amount of acid or base a buffer can neutralize before there is a significant change in pH.

- Ratio of weak base to weak acid ($[A^-]/[HA]$) should be between 0.1 & 10.
- Most effective when $[A^-] = [HA]$ (i.e. ratio = 1)
 - Equal ability to neutralize acids & bases
- Buffer capacity depends on:
 - K_a of the acid
 - Concentration of buffer components
 - More concentrated = higher capacity

$$\text{pH} = \text{pK}_a + \log \frac{[A^-]}{[HA]}$$

pH Range

pH Range: The range of pH values over which a buffer system works effectively

- Best to choose an acid with a pK_a close to the desired pH
- If $[A^-] = [HA]$, then $pH = pK_a$

$$\boxed{pH = pK_a + \log \frac{[A^-]}{[HA]}} \quad \log(1) = 0$$

- Buffer generally usable withing ± 1 pH unit of the pK_a

Criteria for Making a Buffer

1. Choose a weak acid & conjugate base

- Must have the same anion!
 - ex. HNO_2 & NaNO_2 ; HF & LiF

2. Select acid based on desired pH range

- $\text{pK}_a < 7$ buffer is acidic; $\text{pK}_a > 7$ buffer is basic
- Buffers can usually be adjusted to ± 1 desired pH

3. Buffer salts (conjugate base) must be soluble & dissociate completely

- Most commonly sodium or potassium salts
- NH_4^+ salts are acidic because NH_4^+ dissociates

4. Concentrations of $[\text{HA}]$ & $[\text{A}^-] > 0.01\text{M}$

- Must be able to neutralize sufficient acid/base
- Can use ICE table to get an idea of what concentration is needed.

Buffer Calculations: Adding Acid or Base

1. A 1.0 L buffer solution contains 0.150 M nitrous acid and 0.200 M sodium nitrite. $K_a = 7.2 \times 10^{-4}$ (a) What is the pH of the buffer? (b) What is the pH after adding 1.00 g HBr?

A: (a) 3.27

(b) 3.21

Buffer Calculations: Adding Acid or Base

2. A buffer is made by adding 0.600 mol CH_3COOH and 0.600 mol CH_3COONa to enough water to make 2.00L of solution. $K_a = 1.8 \times 10^{-5}$.

(a) What is the pH of the buffer? A: 4.74

(b) Calculate the pH after 0.040 mol HCl is added. A: 4.69

(c) Calculate the pH after 0.040 mol NaOH is added. A: 4.80

Buffer Calculations: Adding Acid or Base

2. A buffer is made by adding 0.600 mol CH_3COOH and 0.600 mol CH_3COONa to enough water to make 2.00L of solution. $K_a = 1.8 \times 10^{-5}$.

(a) What is the pH of the buffer? A: 4.74

(b) Calculate the pH after 0.040 mol HCl is added. A: 4.69

Buffer Calculations: Adding Acid or Base

2. A buffer is made by adding 0.600 mol CH_3COOH and 0.600 mol CH_3COONa to enough water to make 2.00L of solution. $K_a = 1.8 \times 10^{-5}$.

(a) What is the pH of the buffer? A: 4.74

(c) Calculate the pH after 0.040 mol NaOH is added. A: 4.80

Buffer Calculations: Adding Acid or Base

2. A buffer is made by adding 0.600 mol CH_3COOH and 0.600 mol CH_3COONa to enough water to make 2.00L of solution. $K_a = 1.8 \times 10^{-5}$.

(a) What is the pH of the buffer? A: 4.74

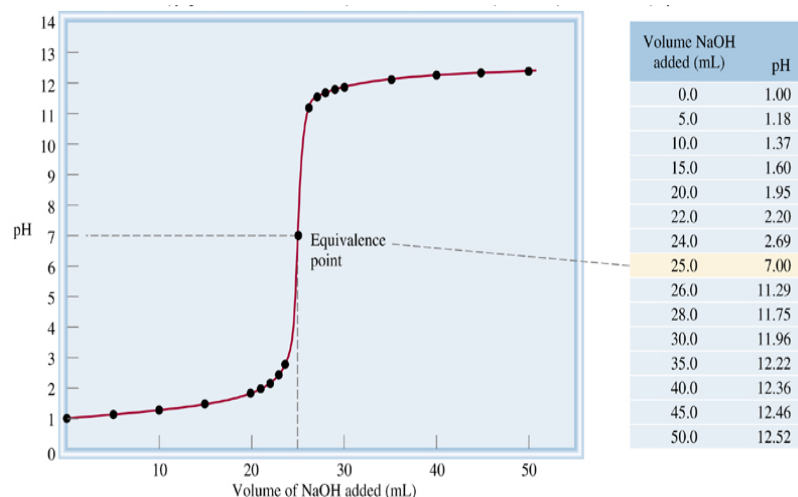
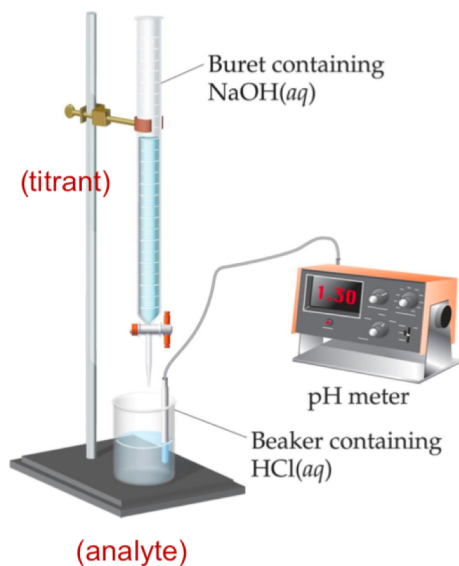
(c) Calculate the pH after 4.00mL of 3.00M HCl is added.

A:4.73

Titration

A technique where a known concentration of acid (or base) is added to a solution of base (or acid).

- Used to determine the concentration of an unknown
- In CHM 101 we looked at strong acid/base systems
 - No equilibrium
 - Equivalence point is pH 7
- Indicators or pH meters are used to determine the equivalence point.

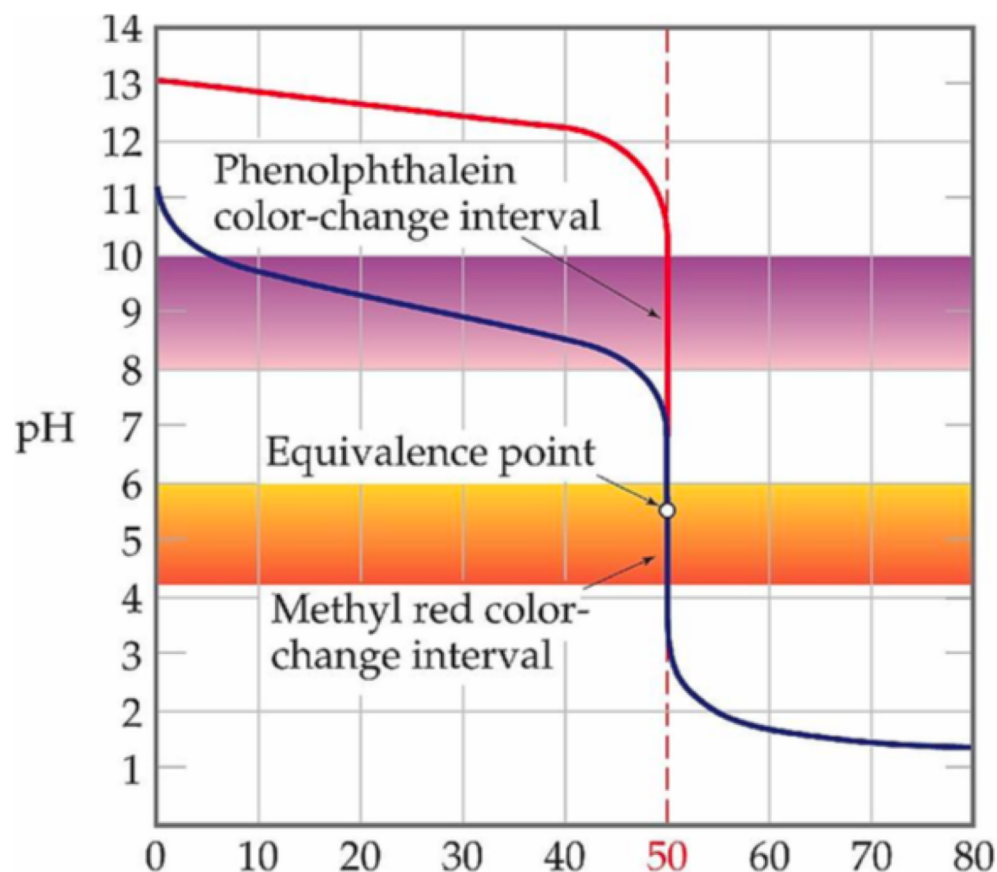


Titration Terminology

Equivalence Point:

Point at which the stoichiometric amount of acid and base are equal.

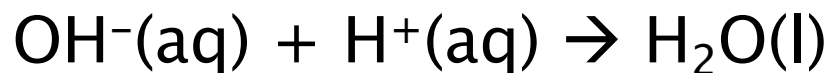
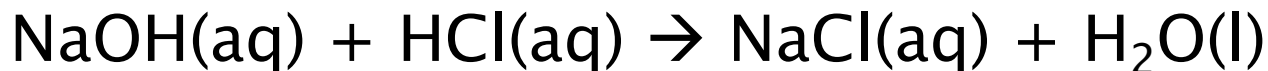
End Point: Point in the titration where the indicator changes color.



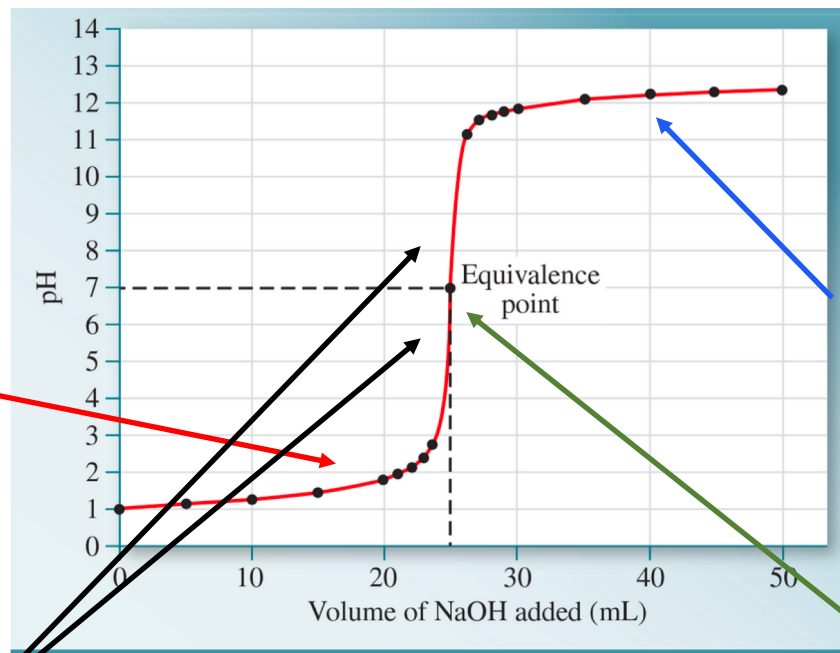
Solving More Complex Titration Problems

- 1. Read the question carefully to see what it is asking**
 - pH or concentration at a particular point
 - Moles or molarity of original solution
 - pH or volume at equivalence point
- 2. Identify all reactants and products**
 - Write the balanced equation
 - Use stoichiometry to determine amounts of products
 - Identify whether the solution is acidic or basic
- 3. Determine whether it is an equilibrium process**
 - You will have at most one equilibrium
 - Strong acids/bases – just stoichiometry
 - Weak acids/bases – stoichiometry + equilibrium
- 4. Volume increases during titrations so be aware that there will likely be changes in concentration due to volume as well as due to the neutralization reaction.**

Titration of a Strong Acid with a Strong Base



From the start of the titration to near the endpoint, the pH increases slowly



As more base is added, the increase in pH again levels off

Just before (and after) the equivalence point, the pH increases rapidly

At the equivalence point, moles acid = moles base
Solution contains only water and salt (neutral)

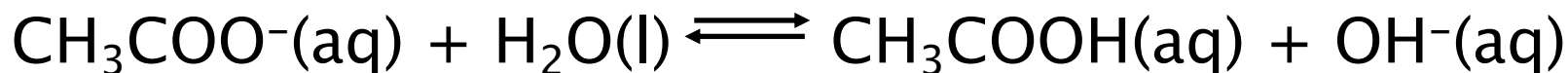
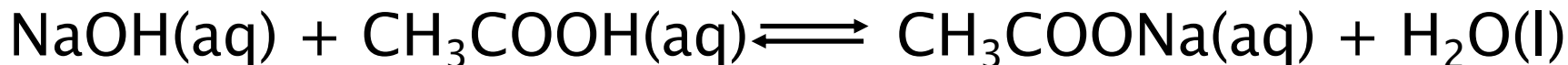
Both strong = NO EQUILIBRIUM

Strong Acid/Strong Base Calculations

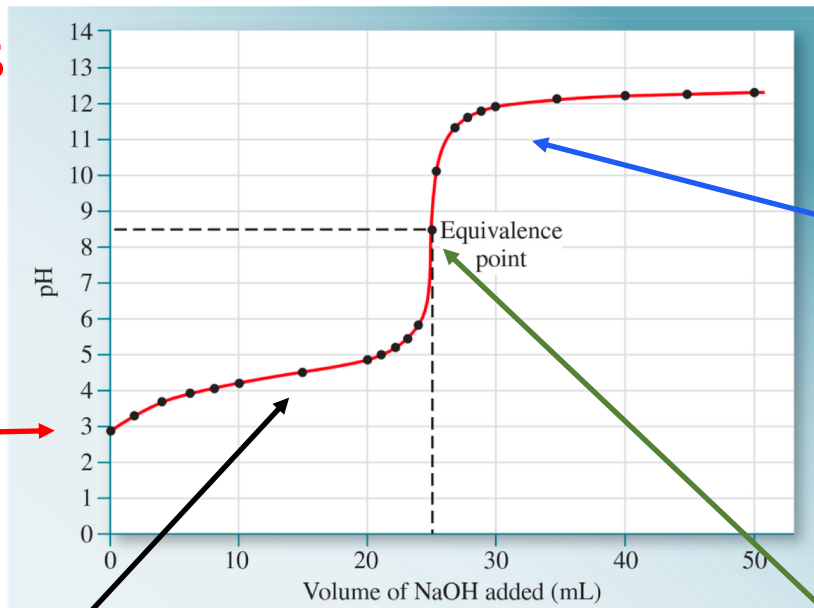
In the titration of 25.0mL of 0.100M KOH with 0.100M HNO_3 , determine the pH:

- (a) At the start of the titration (no acid added) A: 13.0
- (b) When 24.9mL acid has been added A: 10.3
- (c) When 25.1mL acid has been added A: 3.7

Titration of a Weak Acid with a Strong Base



Initially there is only the weak acid; pH depends on concentration & K_a



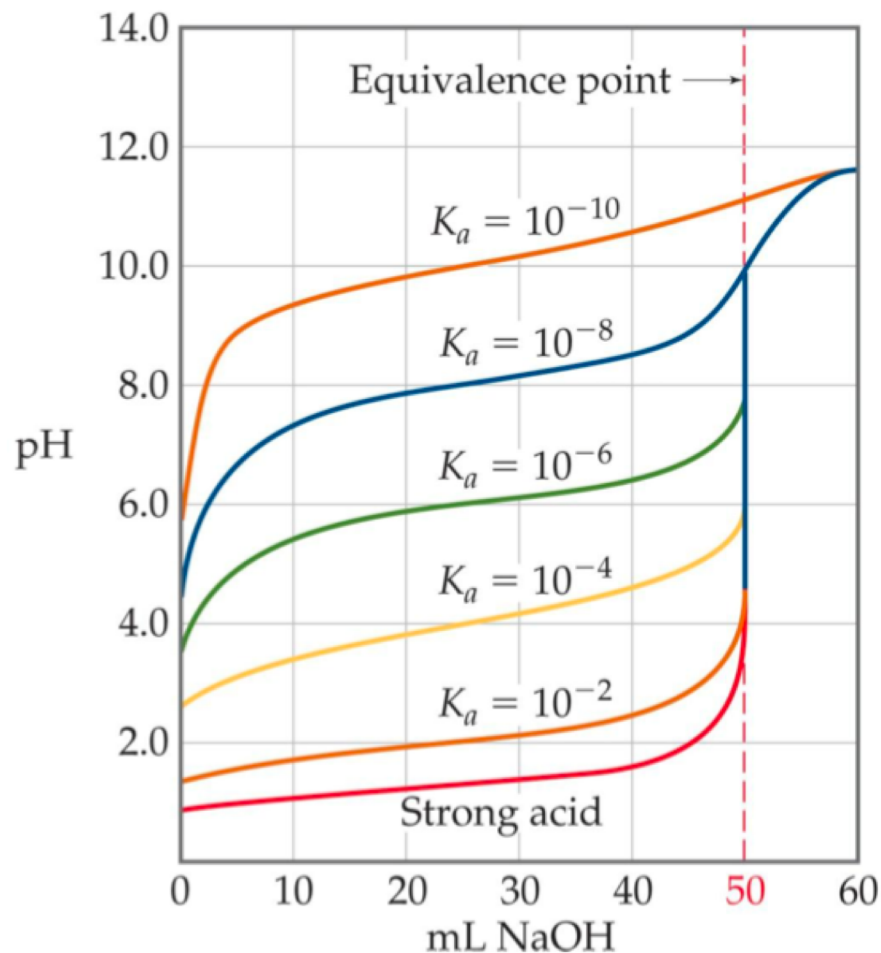
After the equivalence pt., pH depends on concentration of excess strong base

Before the equivalence pt., the solution contains both the weak acid & its conjugate base

At the equivalence pt. (moles acid = moles base) pH is >7 because the conjugate base of the acid affects the pH

pH depends on stoichiometry & Equilibrium!

Titration of a Weak Acid with a Strong Base



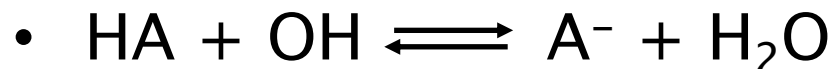
With weak acids:

- Initial pH is higher
- pH changes near the equivalence point are more subtle (smaller)
- pH > 7 at equivalence point due to the formation of a basic salt (conjugate base of weak acid; ex: CH_3COONa)

Weak Acid/Strong Base Calculations

Things to Keep in Mind

1. Acid/Base titration always gives a salt & water



2. Initial pH only depends on the weak acid

- K_a /equilibrium & concentration

3. Addition of base up to just before equivalence point

- Added base is strong – not the conjugate of the weak acid
- Solution contains weak acid & its conjugate base (salt) – all of the strong base is used up in the neutralization
- First use stoichiometry to determine how many moles of the acid have been neutralized
- Determine the new concentration of acid based on moles remaining and new volume (if base is added as a solution)
- Use the equilibrium expression to determine $[\text{H}_3\text{O}^+]$ (can also use H-H if want pH)

4. Whether or not volume increases depends on added base – if the base is in solution, volume increases²⁵

Weak Acid/Strong Base Calculations

Things to Keep in Mind con't

4. At equivalence point: all initial acid & added base are neutralized – the solution only contains the salt

- The salt will be basic – it is the product of a weak acid & a strong base
- The basic salt will react with water to produce OH^-
- $\text{A}^- + \text{H}_2\text{O} \rightleftharpoons \text{HA} + \text{OH}^-$
- Since the solution is basic – need to use K_b & equilibrium to get the OH^- concentration
- Moles acid neutralized = initial moles acid = moles salt formed.
- Use total volume to get concentration.

5. After equivalence point: only excess strong base matters

- pH depends on moles of excess strong base & total volume. Strong so NO EQUILIBRIUM!

Weak Acid/Strong Base Calculations

35.0mL of 0.150M CH_3COOH ($K_a = 1.8 \times 10^{-5}$) was titrated with 0.150M NaOH. Determine the pH:

- a.) At the start of the titration A: 2.78
- b.) When 20.0mL of 0.150M NaOH has been added A: 4.87
- c.) At the equivalence point A: 8.81
- d.) When 50.0mL of 0.150M NaOH has been added A: 12.42

Weak Acid/Strong Base Calculations

35.0mL of 0.150M CH_3COOH ($K_a = 1.8 \times 10^{-5}$) was titrated with 0.150M NaOH. Determine the pH:

b.) When 20.0mL of 0.150M NaOH has been added A:4.87

Weak Acid/Strong Base Calculations

35.0mL of 0.150M CH_3COOH ($K_a = 1.8 \times 10^{-5}$) was titrated with 0.150M NaOH. Determine the pH:

c.) At the equivalence point A: 8.81

Weak Acid/Strong Base Calculations

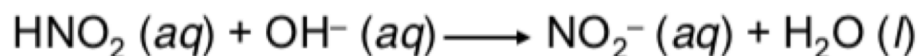
35.0mL of 0.150M CH_3COOH ($K_a = 1.8 \times 10^{-5}$) was titrated with 0.150M NaOH. Determine the pH:

d.) When 50.0mL of 0.150M NaOH has been added A: 12.42

Weak Acid/Strong Base Calculations

When 100.0 mL of 0.10 M HNO_2 are titrated with a 0.10 M NaOH solution, what is the pH at the equivalence point? $K_a \text{HNO}_2 = 4.5 \times 10^{-4}$

start (moles) 0.010 0.010

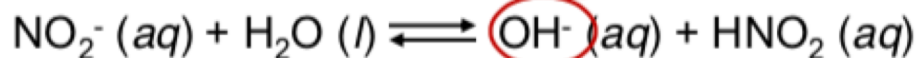


end (moles) 0.0 0.0 0.010

Final volume = 200 mL $\Rightarrow [\text{NO}_2^-] = \frac{0.010}{0.200} = 0.050 \text{ M}$

Use K_b
 $K_b = 2.2 \times 10^{-11}$

Hydrolysis of basic salt



Initial (M) 0.050 0.00 0.00

Change (M) -x +x +x

Equilibrium (M) 0.050 - x x x

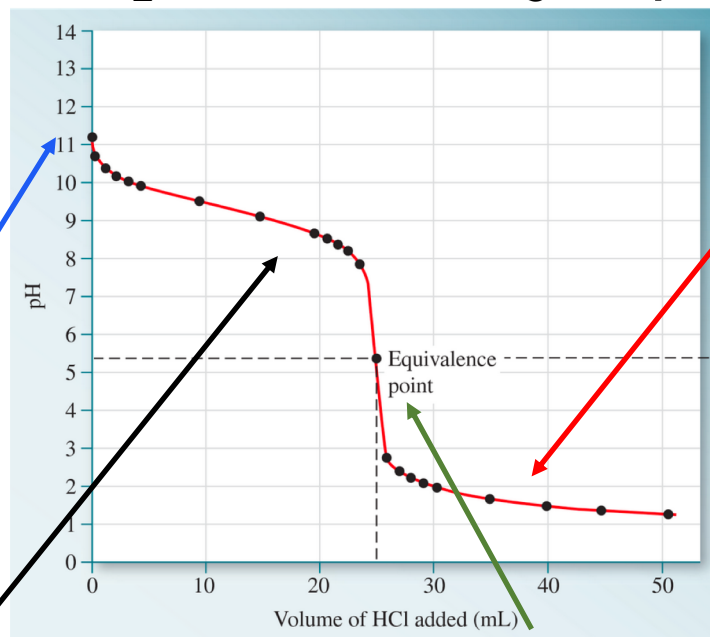
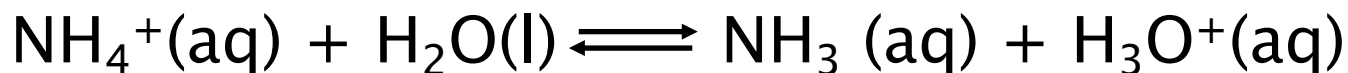
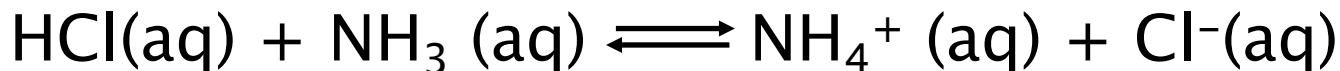
$$K_b = \frac{[\text{OH}^-][\text{HNO}_2]}{[\text{NO}_2^-]} = \frac{x^2}{0.050} = 2.2 \times 10^{-11}$$

$$\text{pOH} = 5.98$$

$$\text{pH} = 14 - 5.98 = 8.02$$

$$x = 1.05 \times 10^{-6} = [\text{OH}^-]$$

Titration of a Weak Base with a Strong Acid



Initially there is only the weak base; pH depends on concentration & K_b

Before the equivalence pt., the solution contains the weak base & its conjugate acid

After the equivalence pt., pH depends on concentration of excess strong acid

At the equivalence pt. (moles acid = moles base) pH is < 7 because the conjugate acid of the base affects the pH

pH depends on stoichiometry & Equilibrium!

Weak Base/Strong Acid Calculations

30.0mL of 0.0300M NH_3 ($K_b = 1.8 \times 10^{-5}$) was titrated with 0.0250M HCl. Determine the pH:

- a.) At the start of the titration A: 10.87
- b.) When 20.0mL of 0.0250M HCl has been added A: 9.16
- c.) At the equivalence point A: 5.56
- d.) When 37.0mL of 0.025M HCl has been added A: 3.43

a.) At the start of the titration (no acid added) – just a solution of a weak base – pH depends on concentration & equilibrium



I	0.03M	0	0	$K_b = \frac{x^2}{0.0300} = 1.8 \times 10^{-5}$
C	-x	+x	+x	
E	0.03-x	x	x	

$$x^2 = 5.4 \times 10^{-7}$$

$$\text{pOH} = -\log (7.35 \times 10^{-4}) = 3.13$$

$$x = 7.35 \times 10^{-4} = [\text{OH}^-]$$

$$\text{pH} = 14 - 3.13 = 10.87$$

Weak Base/Strong Acid Calculations

30.0mL of 0.0300M NH_3 ($K_b = 1.8 \times 10^{-5}$) was titrated with 0.0250M HCl. Determine the pH:

b.) When 20.0mL of 0.0250M HCl has been added **A: 9.16**

• All added HCl is used in the titration – need to determine how much NH_3 remains & how much NH_4^+ has been produced.



$$0.0300 \frac{\text{mol}}{\text{L}} \text{NH}_3 \times 0.0300\text{L} = 9.00 \times 10^{-4} \text{mol NH}_3 \text{ initial}$$

$$0.0250 \frac{\text{mol}}{\text{L}} \times 0.0200\text{L} = 5.00 \times 10^{-4} \text{mol HCl added}$$

$$5.00 \times 10^{-4} \text{mol HCl} \times \frac{1 \text{mol NH}_3}{1 \text{mol HCl}} = 5.00 \times 10^{-4} \text{mol NH}_3 \text{ neutralized}$$

$$9.00 \times 10^{-4} \text{mol init.} - 5.00 \times 10^{-4} \text{mol neut.} = 4.00 \times 10^{-4} \text{mole NH}_3 \text{ remaining}$$

$$5.00 \times 10^{-4} \text{mol HCl} \times \frac{1 \text{mol NH}_4^+}{1 \text{mol HCl}} = 5.00 \times 10^{-4} \text{mol NH}_4^+ \text{ produced}$$

$$\text{New volume: } 0.0300\text{L} + 0.0200\text{L} = 0.0500\text{L}$$

$$4.00 \times 10^{-4} \text{mol NH}_3 / 0.0500\text{L} = 8.00 \times 10^{-3} \text{M NH}_3$$

$$5.00 \times 10^{-4} \text{mol NH}_4^+ / 0.0500\text{L} = 1.00 \times 10^{-2} \text{M NH}_4^+$$

$$4.00 \times 10^{-4} \text{ mol NH}_3 / 0.0500 \text{ L} = 8.00 \times 10^{-3} \text{ M NH}_3$$

$$5.00 \times 10^{-4} \text{ mol NH}_4^+ / 0.0500 \text{ L} = 1.00 \times 10^{-2} \text{ M NH}_4^+$$

New equilibrium with NH_3 & NH_4^+ present:



I	0.008M		0.01M	0
C	-x		+x	+x
E	0.008- x		0.01 + x	x

$$K_b = \frac{(0.01)(x)}{0.008} = 1.8 \times 10^{-5}$$

$$0.01x = 1.44 \times 10^{-7}$$

$$x = 1.44 \times 10^{-7} / 0.01 = 1.44 \times 10^{-5} = [\text{OH}^-]$$

$$\text{pOH} = -\log(1.44 \times 10^{-5}) = 4.84164$$

$$\text{pH} = 14 - 4.84164 = 9.1594 \rightarrow \mathbf{9.16}$$

Could also use the NH_3 & NH_4^+ molarities listed above in the H-H eq – but for H-H would need to use pKa and make sure to have $[\text{A}^-]$ and $[\text{HA}]$ in the correct locations

Weak Base/Strong Acid Calculations

30.0mL of 0.0300M NH_3 ($K_b = 1.8 \times 10^{-5}$) was titrated with 0.0250M HCl. Determine the pH:

c.) At the equivalence point **A: 5.56**

- At the equivalence point, moles added acid = initial moles base
- All added acid & initial base are neutralized (i.e. all NH_3 became NH_4^+)
- pH depends on equilibrium of CONJUGATE acid

Conjugate acid of NH_3 is NH_4^+ .

Moles NH_4^+ = moles NH_3 neutralized: $0.0300 \frac{\text{mol}}{\text{L}} \times 0.0300\text{L} = 9.00 \times 10^{-4} \text{mol}$

Volume acid needed for neutralization = volume containing 9.00×10^{-4} mol HCl: $9.00 \times 10^{-4} \text{mol HCl} \times \frac{1\text{L HCl}}{0.0250 \text{mol HCl}} = 0.036\text{L HCl solution}$

Total volume = 0.0360L added + 0.0300L initial = 0.0660L

Concentration of NH_4^+ = $9.00 \times 10^{-4} \text{mol} / 0.0660\text{L} = 0.013636\text{M}$

Equilibrium is:





I	0.013536	0	0
C	-x	+x	+x
E	0.013636 - x	x	x

$$K_a = \frac{K_w}{K_b} = \frac{1.00 \times 10^{-14}}{1.8 \times 10^{-5}} = 5.56 \times 10^{-10}$$

$$K_a = \frac{x^2}{0.013636} = 5.56 \times 10^{-10}$$

$$x^2 = 7.576 \times 10^{-12}$$

$$x = 2.752 \times 10^{-6} = [\text{H}_3\text{O}^+]$$

$$\text{pH} = -\log (2.752 \times 10^{-6}) = 5.5603 \rightarrow 5.56$$

Weak Base/Strong Acid Calculations

30.0mL of 0.0300M NH_3 ($K_b = 1.8 \times 10^{-5}$) was titrated with 0.0250M HCl. Determine the pH:

d.) When 37.0mL of 0.025M HCl has been added **A: 3.43**

- Excess HCl has been added. HCl is strong. pH depends on amount of HCl left over after neutralization.
- Strong acid = no equilibrium

Reaction: $\text{NH}_3(\text{aq}) + \text{HCl}(\text{aq}) \rightarrow \text{NH}_4^+(\text{aq}) + \text{Cl}^-(\text{aq})$

Moles HCl added: $\frac{0.0250 \text{ mol HCl}}{1 \text{ L}} \times 0.0370 \text{ L} = 9.25 \times 10^{-4} \text{ mol HCl}$

Moles HCl needed for neutralization:

$$9.00 \times 10^{-4} \text{ mol NH}_3 \times \frac{1 \text{ mol HCl}}{1 \text{ mol NH}_3} = 9.00 \times 10^{-4} \text{ mol HCl}$$

Moles HCl not used in neutralization:

$$9.25 \times 10^{-4} \text{ mol added} - 9.00 \times 10^{-4} \text{ mol used} = 2.5 \times 10^{-5} \text{ mol HCl left over}$$

$$\text{Total volume} = 0.0300 \text{ L} + 0.0370 \text{ L} = 0.0670 \text{ L}$$

$$\text{Concentration of HCl} = 2.5 \times 10^{-5} \text{ mol} / 0.0670 \text{ L} = 3.73 \times 10^{-4} \text{ M}$$

$$\text{Strong acid so } [\text{H}_3\text{O}^+] = 3.73 \times 10^{-4} \text{ M} \quad \text{pH} = -\log(3.73 \times 10^{-4}) = 3.43$$

Acid–Base Indicators

Chemical added during a titration to cause a color change at a particular pH allowing the user to detect the endpoint.

Things to consider when choosing an indicator:

Example: titration of CH_3COOH with NaOH

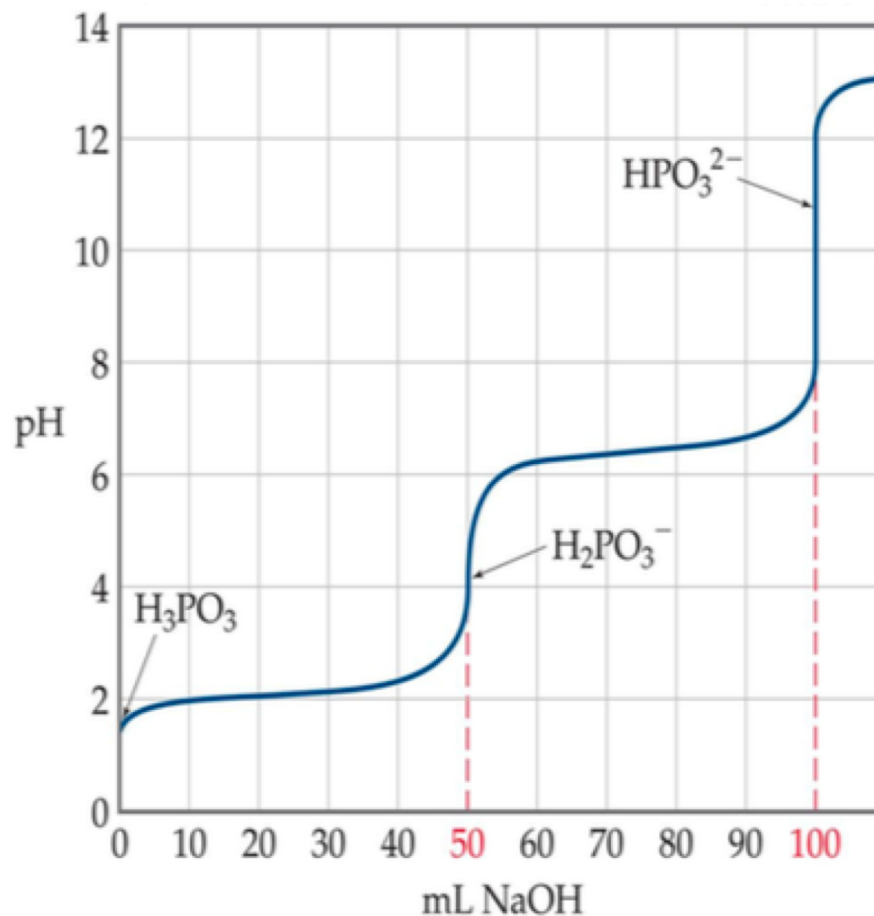
- What kind of titration is it? Weak acid with strong base
- What kind of salt is formed? Basic salt
- What happens to pH due to hydrolysis? Salt is basic so $\text{pH} > 7.0$

TABLE 17.1 Some Common Acid-Base Indicators

Indicator	Color		pH Range*
	In Acid	In Base	
Thymol blue	Red	Yellow	1.2–2.8
Bromophenol blue	Yellow	Bluish purple	3.0–4.6
Methyl orange	Orange	Yellow	3.1–4.4
Methyl red	Red	Yellow	4.2–6.3
Chlorophenol blue	Yellow	Red	4.8–6.4
Bromothymol blue	Yellow	Blue	6.0–7.6
Cresol red	Yellow	Red	7.2–8.8
Phenolphthalein	Colorless	Reddish pink	8.3–10.0

*The pH range is defined as the range over which the indicator changes from the acid color to the base color.

Titration of Polyprotic Acids



The titration of a polyprotic acid with a base will give an equivalence point for each acidic proton.

Solubility Equilibria

Aqueous Salt Solutions & Solubility

CHM 101

- Ionic compounds were considered soluble or insoluble
- Soluble compounds dissociated fully in water
- Basic stoichiometry rules were used

CHM 112

- Most ionic compounds are “slightly” soluble – they do dissolve a little, but not very much
- A small amount of dissolved & dissociated material is present with the bulk undissolved
- Ions are constantly moving between the dissolved and undissolved states – **EQUILIBRIUM!**
- Solubility constant is K_{sp} (solubility product constant)
- Discussed in terms of Molar Solubility –
 - moles solute/ 1L saturated solution

CHM 101 Solubility Rules for ions

Soluble

Ammonium (NH_4^+)
Hydrogen (H^+)
Alkali metals (group 1A)
Nitrate (NO_3^-)
Perchlorate (ClO_4^-)
Acetate (CH_3COO^-)

Always
soluble

**Usually
Soluble**

Halides (F^- , Cl^- , Br^- , & I^-)

Exceptions (insoluble if with):
 Pb^{2+} , Hg_2^{2+} , Ag^+

Sulfate (SO_4^{2-})

Pb^{2+} , Hg_2^{2+} , Ag^+ , Ba^{2+} , Ca^{2+} , Sr^{2+}

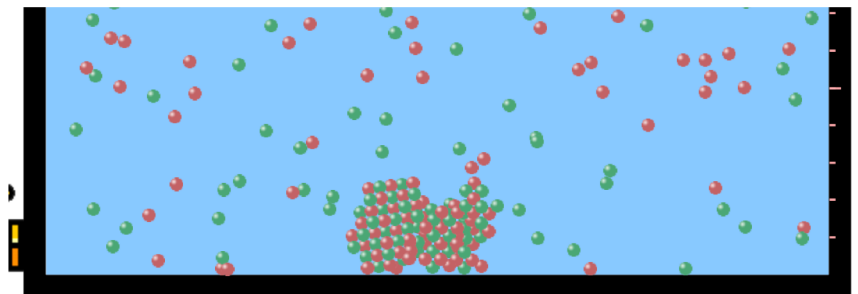
**Sparingly
Soluble
(Insoluble)**

Sulfide (S^{2-})
Hydroxide (OH^-)
Oxide (O^{2-})
Carbonate (CO_3^{2-})
Phosphate (PO_4^{3-})

Exceptions:
soluble if with any of
the cations listed in the
always soluble box

Solubility Product Constant (K_{sp})

A slightly soluble ionic material is placed in water.



- The solubility is low so most will not dissolve
- What does dissolve will dissociate into ions



- The solid is in equilibrium with the dissolved ions
- The equilibrium expression is:

$$K_{sp} = [\text{Pb}^{2+}][\text{Cl}^{-}]^2$$

- Note that the $\text{PbCl}_2(\text{s})$ is not included in the equilibrium expression. Why?

Solubility Product Constant (K_{sp})

- K_{sp} is an approximation used to estimate solubility
- Measures the extent to which a substance will dissolve in water
- Larger K_{sp} = higher solubility
- Amount of solid material present does not alter K_{sp}
 - Solids are not included in equilibrium expressions!

TABLE 17.2 Solubility Products of Some Slightly Soluble Ionic Compounds at 25°C

Compound	K_{sp}	Compound	K_{sp}
Aluminum hydroxide $[\text{Al}(\text{OH})_3]$	1.8×10^{-33}	Lead(II) chromate (PbCrO_4)	2.0×10^{-14}
Barium carbonate (BaCO_3)	8.1×10^{-9}	Lead(II) fluoride (PbF_2)	4.1×10^{-8}
Barium fluoride (BaF_2)	1.7×10^{-6}	Lead(II) iodide (PbI_2)	1.4×10^{-8}
Barium sulfate (BaSO_4)	1.1×10^{-10}	Lead(II) sulfide (PbS)	3.4×10^{-28}
Bismuth sulfide (Bi_2S_3)	1.6×10^{-72}	Magnesium carbonate (MgCO_3)	4.0×10^{-5}
Cadmium sulfide (CdS)	8.0×10^{-28}	Magnesium hydroxide $[\text{Mg}(\text{OH})_2]$	1.2×10^{-11}
Calcium carbonate (CaCO_3)	8.7×10^{-9}	Manganese(II) sulfide (MnS)	3.0×10^{-14}
Calcium fluoride (CaF_2)	4.0×10^{-11}	Mercury(I) chloride (Hg_2Cl_2)	3.5×10^{-18}
Calcium hydroxide $[\text{Ca}(\text{OH})_2]$	8.0×10^{-6}	Mercury(II) sulfide (HgS)	4.0×10^{-54}
Calcium phosphate $[\text{Ca}_3(\text{PO}_4)_2]$	1.2×10^{-26}	Nickel(II) sulfide (NiS)	1.4×10^{-24}
Chromium(III) hydroxide $[\text{Cr}(\text{OH})_3]$	3.0×10^{-29}	Silver bromide (AgBr)	7.7×10^{-13}
Cobalt(II) sulfide (CoS)	4.0×10^{-21}	Silver carbonate (Ag_2CO_3)	8.1×10^{-12}
Copper(I) bromide (CuBr)	4.2×10^{-8}	Silver chloride (AgCl)	1.6×10^{-10}
Copper(I) iodide (CuI)	5.1×10^{-12}	Silver iodide (AgI)	8.3×10^{-17}
Copper(II) hydroxide $[\text{Cu}(\text{OH})_2]$	2.2×10^{-20}	Silver sulfate (Ag_2SO_4)	1.4×10^{-5}
Copper(II) sulfide (CuS)	6.0×10^{-37}	Silver sulfide (Ag_2S)	6.0×10^{-51}
Iron(II) hydroxide $[\text{Fe}(\text{OH})_2]$	1.6×10^{-14}	Strontium carbonate (SrCO_3)	1.6×10^{-9}
Iron(III) hydroxide $[\text{Fe}(\text{OH})_3]$	1.1×10^{-36}	Strontium sulfate (SrSO_4)	3.8×10^{-7}
Iron(II) sulfide (FeS)	6.0×10^{-19}	Tin(II) sulfide (SnS)	1.0×10^{-26}
Lead(II) carbonate (PbCO_3)	3.3×10^{-14}	Zinc hydroxide $[\text{Zn}(\text{OH})_2]$	1.8×10^{-14}
Lead(II) chloride (PbCl_2)	2.4×10^{-4}	Zinc sulfide (ZnS)	3.0×10^{-23}

Calculating K_{sp} from Solubility

The molar solubility of CaF_2 at 35°C is $1.24 \times 10^{-3} \text{ M}$.

(a) What is the solubility of CaF_2 in g/L? A: 0.0968 g/L

(b) What is K_{sp} at this temperature? A: 7.63×10^{-9}

Calculating Solubility from K_{sp}

The K_{sp} for LaF_3 is 2.0×10^{-19} .

(a) What is the molar solubility of LaF_3 in water? A: $9.3 \times 10^{-6} \text{M}$

(b) What is the solubility in g/L? A: $1.8 \times 10^{-3} \text{g/L}$

Comparing Molar Solubilities vs. K_{sp}

Compound	K_{sp}	Molar Solubility
BaSO_4	1.1×10^{-10}	$1.0 \times 10^{-5} \text{M}$
$\text{Mg}_3(\text{AsO}_4)_2$	2.0×10^{-20}	$5.0 \times 10^{-5} \text{M}$

Molar Solubility Comparison:

$\text{Mg}_3(\text{AsO}_4)_2$ molar solubility is 5X greater than BaSO_4

K_{sp} Comparison

BaSO_4 has a K_{sp} that is 10^9 X greater than $\text{Mg}_3(\text{AsO}_4)_2$

Be careful using K_{sp} directly to compare solubilities

- Number of ions present also matters
- Can only directly compare K_{sp} if # ions produced is identical

Factors Affecting Solubility:

Common-Ion Effect

- One of the ions in the compound is also part of another compound present in the solution

pH

- Presence of hydroxide (OH^-) or hydronium ions (H_3O^+)

Complexation

- Formation of coordinate bonds with solvent or other molecules present in solution


Common-Ion Effect

The extent of ionization of a weak electrolyte is decreased by the addition of a strong electrolyte that has an ion in common with the weak electrolyte.

Equilibrium process – presence of ions shifts process back to reactants.

Ex: A solution is made with 1.0M CaCl_2 and 2.0M Ca(OH)_2



 Add extra Ca^{2+} from CaCl_2
Shift equilibrium

For solubility equilibria, the presence of a common ion will decrease the solubility of the slightly soluble compound.

1. The K_{sp} of $Mn(OH)_2$ is 1.6×10^{-13} . Calculate the molar solubility of $Mn(OH)_2$ in:

a.) water A: $3.4 \times 10^{-5} M$

b.) A solution that contains 0.020M NaOH A: $4.0 \times 10^{-10} M$

c.) Compare the solubility of $Mn(OH)_2$ in these solutions
A: 85,000 times more soluble in water

2.) How much is the solubility of lead (II) chloride changed in the presence of 0.85M NaCl? $K_{sp} = 1.6 \times 10^{-5}$

More than 700X less
soluble than in water

Effect of pH

If the Compound Contains a(n):

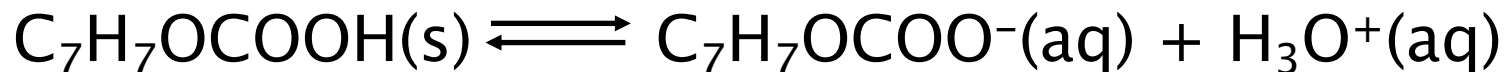
- **Basic Anion:** More soluble in acidic solution



In acidic solution: $\text{OH}^{-}(\text{aq}) + \text{H}_3\text{O}^{+}(\text{aq}) \rightleftharpoons 2\text{H}_2\text{O}(\text{l})$

OH^{-} removed from solution, dissolution equilibrium shifts toward more dissolved product

- **Acidic Cation:** More soluble in basic solution



In basic solution: $\text{H}_3\text{O}^{+}(\text{aq}) + \text{OH}^{-}(\text{aq}) \rightleftharpoons 2\text{H}_2\text{O}(\text{l})$

H_3O^{+} removed from solution, dissolution equilibrium shifts toward more dissolved product

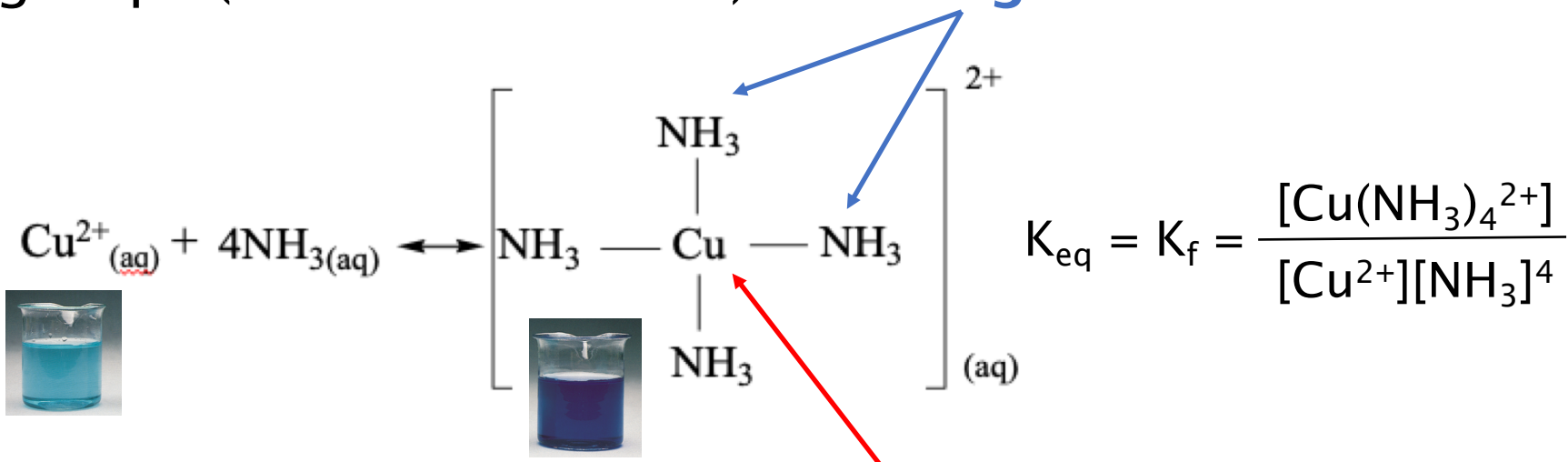
Effect of pH Calculations

Calculate the solubility of $\text{Mg}(\text{OH})_2$ (one of the ingredients in the antacid Maalox) in grams per liter when buffered at pH: (a) 12.50; (b) 7.00 A: a.) $7.01 \times 10^{-7} \text{ g/L}$; b.) $7.00 \times 10^{-4} \text{ g/L}$

K_{sp} of $\text{Mg}(\text{OH})_2 = 1.2 \times 10^{-11}$; MM $\text{Mg}(\text{OH})_2 = 58.32 \text{ g/mol}$

Complex Ion Formation

Complex Ion: A central metal ion surrounded by other groups (molecules or ions) called **ligands**.



The metal center (Cu) is a **Lewis Acid** that accepts electron pairs from the ligands (NH_3), which act as **Lewis Bases** by donating electron pairs.

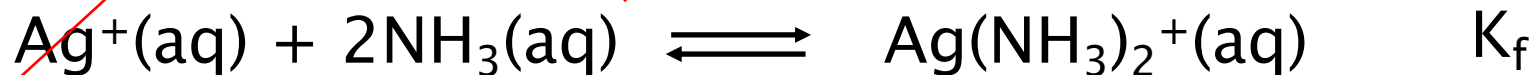
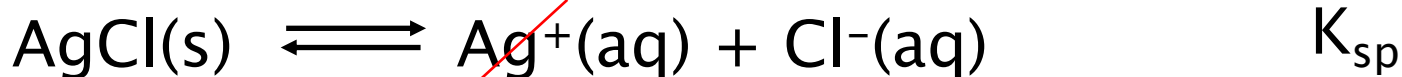
Formation of a complex ion is a reversible equilibrium reaction with its own equilibrium constant, K_{f} .

K_{f} = formation constant

Common Complex Ion Ligands: NH_3 , CN^- , OH^- , Br^- , I^-

Complex Ion Formation & Solubility

Formation of a Complex Ion can increase solubility



- Ag^+ is removed from solution, shifting solubility equilibrium to the dissociated products
- More AgCl(s) dissolves
- K_{sp} governs first process
- K_{f} governs second process
- Two processes are added together
- K_{c} (overall equilibrium expression) = $K_{\text{sp}} \times K_{\text{f}}$

K_f Values for Selected Complex Ions

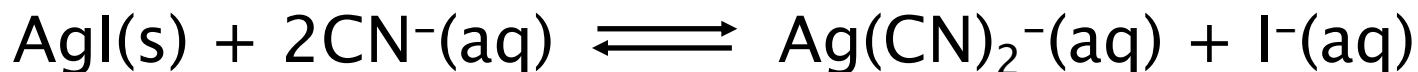
TABLE 18.5

Formation Constants of Selected Complex Ions in Water at 25°C

Complex Ion	Equilibrium Expression	Formation Constant (K_f)
$\text{Ag}(\text{NH}_3)_2^+$	$\text{Ag}^+ + 2\text{NH}_3 \rightleftharpoons \text{Ag}(\text{NH}_3)_2^+$	1.5×10^7
$\text{Ag}(\text{CN})_2^-$	$\text{Ag}^+ + 2\text{CN}^- \rightleftharpoons \text{Ag}(\text{CN})_2^-$	1.0×10^{21}
$\text{Cu}(\text{CN})_4^{2-}$	$\text{Cu}^{2+} + 4\text{CN}^- \rightleftharpoons \text{Cu}(\text{CN})_4^{2-}$	1.0×10^{25}
$\text{Cu}(\text{NH}_3)_4^{2+}$	$\text{Cu}^{2+} + 4\text{NH}_3 \rightleftharpoons \text{Cu}(\text{NH}_3)_4^{2+}$	5.0×10^{13}
$\text{Cd}(\text{CN})_4^{2-}$	$\text{Cd}^{2+} + 4\text{CN}^- \rightleftharpoons \text{Cd}(\text{CN})_4^{2-}$	7.1×10^{16}
CdI_4^{2-}	$\text{Cd}^{2+} + 4\text{I}^- \rightleftharpoons \text{CdI}_4^{2-}$	2.0×10^6
HgCl_4^{2-}	$\text{Hg}^{2+} + 4\text{Cl}^- \rightleftharpoons \text{HgCl}_4^{2-}$	1.7×10^{16}
HgI_4^{2-}	$\text{Hg}^{2+} + 4\text{I}^- \rightleftharpoons \text{HgI}_4^{2-}$	2.0×10^{30}
$\text{Hg}(\text{CN})_4^{2-}$	$\text{Hg}^{2+} + 4\text{CN}^- \rightleftharpoons \text{Hg}(\text{CN})_4^{2-}$	2.5×10^{41}
$\text{Co}(\text{NH}_3)_6^{3+}$	$\text{Co}^{3+} + 6\text{NH}_3 \rightleftharpoons \text{Co}(\text{NH}_3)_6^{3+}$	5.0×10^{31}
$\text{Zn}(\text{NH}_3)_4^{2+}$	$\text{Zn}^{2+} + 4\text{NH}_3 \rightleftharpoons \text{Zn}(\text{NH}_3)_4^{2+}$	2.9×10^9
$\text{Cr}(\text{OH})_4^-$	$\text{Cr}^{3+} + 4\text{OH}^- \rightleftharpoons \text{Cr}(\text{OH})_4^-$	8×10^{29}

Complex Ion Formation & Solubility

1. Determine the equilibrium constant for the reaction:



$$K_{\text{sp}} \text{ AgI} = 8.3 \times 10^{-17}; K_{\text{f}} \text{ Ag(CN)}_2^{-} = 1 \times 10^{21}$$

Complex Ion Formation & Solubility

2. Calculate the molar solubility of zinc carbonate at 25°C in (a) pure water and (b) 1.0M NH_3

$K_{\text{sp}} = 1.4 \times 10^{-11}$; $K_{\text{f}} = 4.1 \times 10^8$ for $\text{Zn}(\text{NH}_3)_4^{2+}$

A: (a) $3.7 \times 10^{-6}\text{M}$

(b) $7.6 \times 10^{-2}\text{M}$

Prediction of Precipitation

Whether or not a precipitate will form depends on concentration.

Can use Q_c values to predict precipitate formation

Calculate Q_c based on given concentrations & compare Q_c to K_{sp}

- $Q_c > K_{sp}$ Concentration too high \rightarrow Precipitate will form
- $Q_c < K_{sp}$ Concentration low \rightarrow all ions remain in solution
- $Q_c = K_{sp}$ At Equilibrium \rightarrow saturated solution

Prediction of Precipitation

1.) If 2.00mL of 0.200M NaOH are added to 1.00L of 0.100M CaCl_2 , will a precipitate form? **A: no precipitate will form**

Prediction of Precipitation

2.) How many grams of solid K_2SO_4 (174.3g/mol) would need to be added to 50.0mL of a 0.0010M $\text{Ca}(\text{NO}_3)_2$ solution in order to (a) start precipitation and (b) precipitate 99% of the calcium?

A: 0.079g

Prediction of Precipitation

2.) How many grams of solid K_2SO_4 (174.3g/mol) would need to be added to 50.0mL of a 0.0010M $\text{Ca}(\text{NO}_3)_2$ solution in order to (a) start precipitation and (b) precipitate 99% of the calcium?

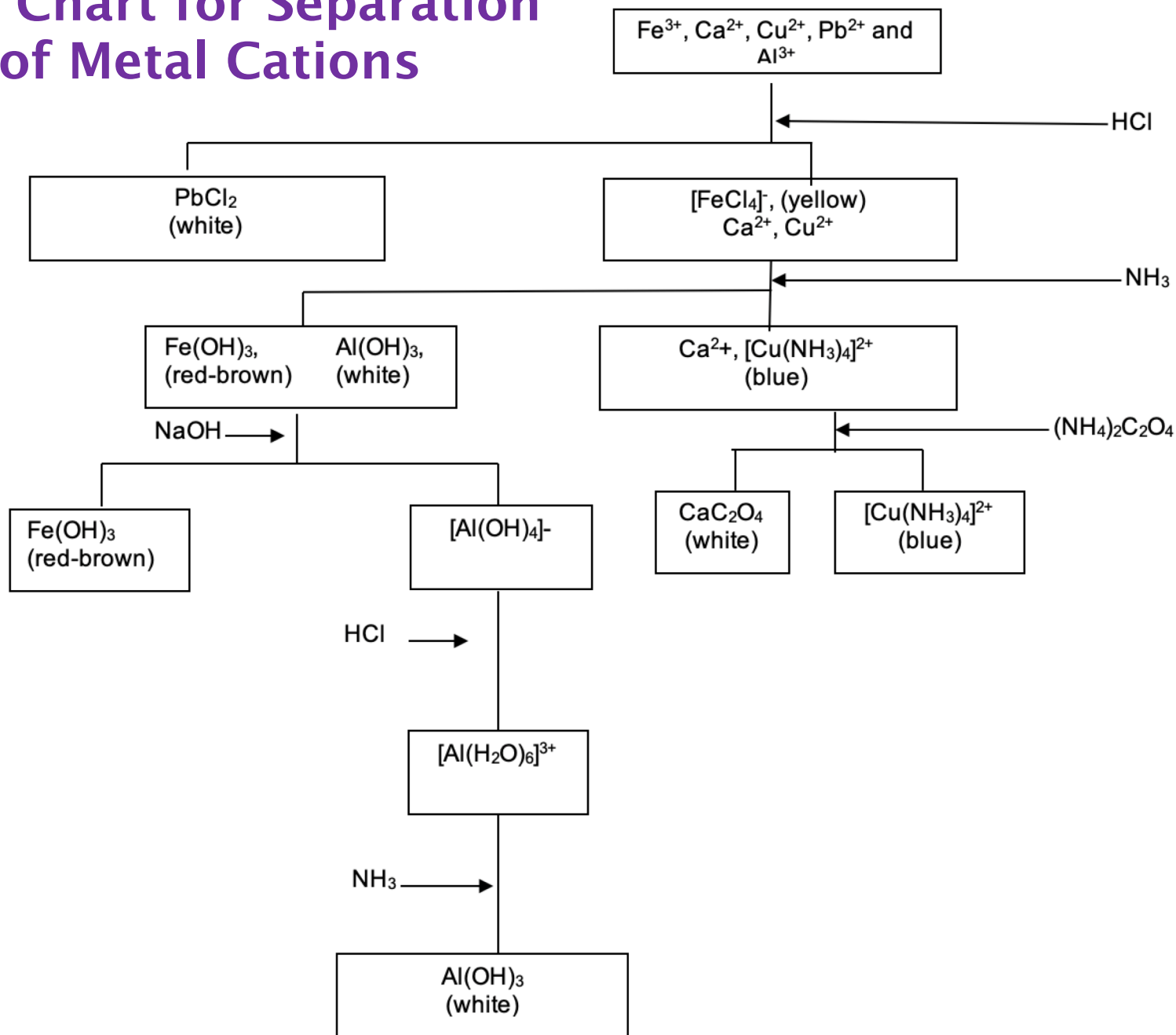
Qualitative Analysis of Metal Ions

Ways to determine which ions are present in solution

- **Selective (fractional) precipitation**
 - One compound has very low K_{sp} and will form a precipitate
 - Other compounds have very high (or no) K_{sp}
- **Complex formation**
 - Ligands will only form complex with one ion present
 - May cause a precipitate to dissolve
- **Flame tests**
 - Color of flame can be used for ID
 - CHM 101 – energy levels!

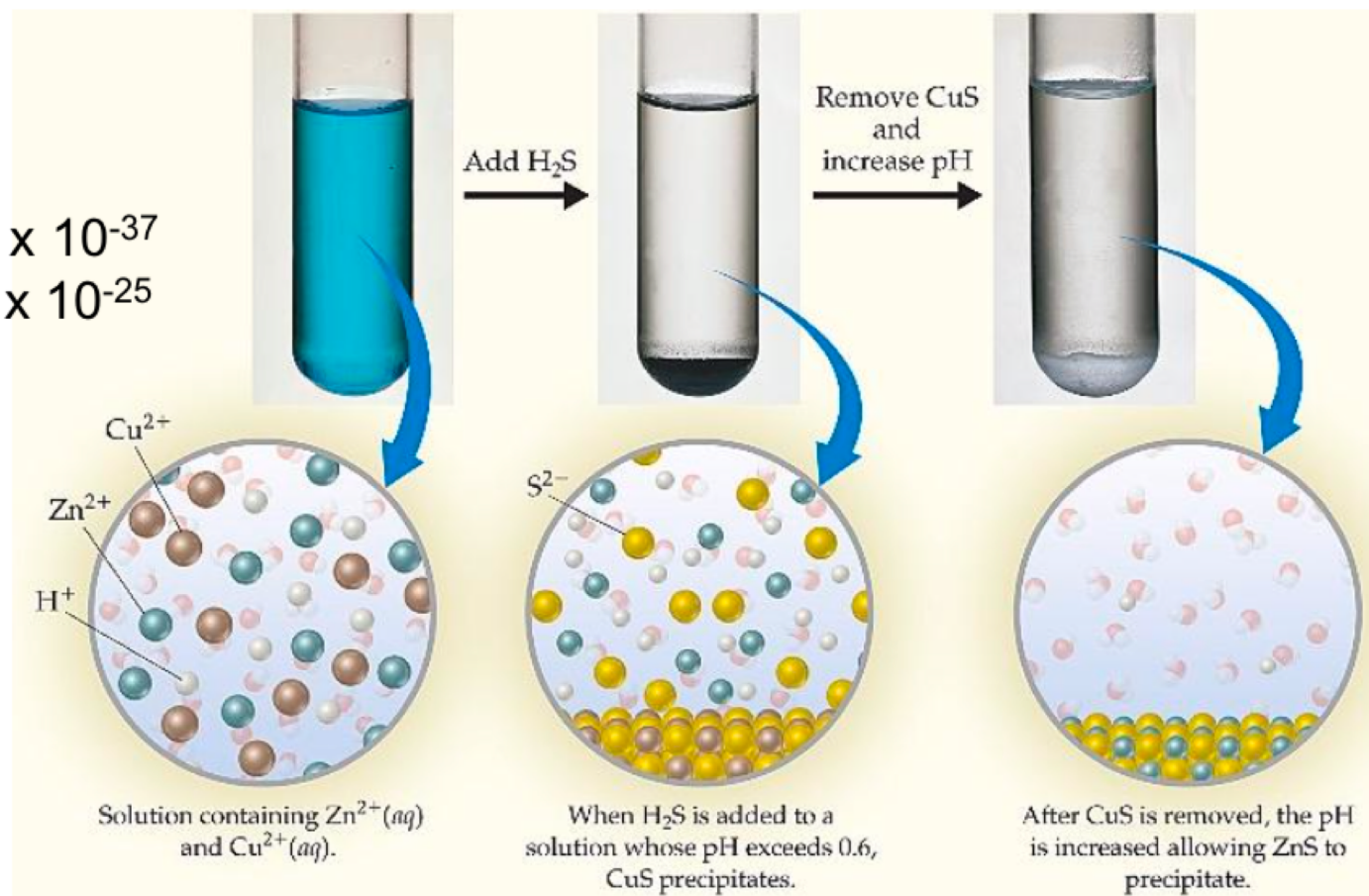


Flow Chart for Separation of Metal Cations



Selective Precipitation

K_{sp} :
 $\text{CuS} = 6 \times 10^{-37}$
 $\text{ZnS} = 2 \times 10^{-25}$



Solution contains
 $\text{Zn}^{2+}(\text{aq})$ & $\text{Cu}^{2+}(\text{aq})$

H_2S is added
At low pH (but > 0.6)
CuS precipitates

CuS is removed
then pH is
increased causing
ZnS to precipitate

Selective Precipitation

A solution contains 0.050M Mg^{2+} and 0.020M Cu^{2+} . Solid NaOH is added to the solution. $K_{\text{sp}} \text{Mg}(\text{OH})_2 = 1.8 \times 10^{-11}$;
 $K_{\text{sp}} \text{Cu}(\text{OH})_2 = 4.8 \times 10^{-20}$

(a) Which ion will precipitate first? A: Cu^{2+}

(b) What concentration of OH^- is necessary to begin precipitation of each cation. A: Cu^{2+} needs $1.5 \times 10^{-9}\text{M}$
 Mg^{2+} needs $1.9 \times 10^{-5}\text{M}$

Selective Precipitation

A solution contains 0.050M Mg^{2+} and 0.020M Cu^{2+} . Solid NaOH is added to the solution. $K_{\text{sp}} \text{Mg}(\text{OH})_2 = 1.8 \times 10^{-11}$;
 $K_{\text{sp}} \text{Cu}(\text{OH})_2 = 4.8 \times 10^{-20}$

A: Cu^{2+} needs $1.5 \times 10^{-9}\text{M}$
 Mg^{2+} needs $1.9 \times 10^{-5}\text{M}$

(a) What concentration of OH^- is necessary to begin precipitation of each cation.



$$K_{\text{sp}} = [0.020][\text{X}]^2 = 4.8 \times 10^{-20}$$

$$\text{X}^2 = 2.4 \times 10^{-18}$$

$$\text{X} = [\text{OH}] = 1.5 \times 10^{-9}\text{M}$$

$$K_{\text{sp}} = [0.020][2\text{X}]^2 = 4.8 \times 10^{-20}$$

$$K_{\text{sp}} = 0.080\text{X}^2 = 4.8 \times 10^{-20}$$

$$\text{X}^2 = 6.0 \times 10^{-19}$$

$$\text{X} = 7.75 \times 10^{-10}\text{M}$$

$$[\text{OH}] = 2\text{X} = 2(7.75 \times 10^{-10}\text{M})$$

$$[\text{OH}] = 1.5 \times 10^{-9}\text{M}$$