

# Chapter Thirteen

## Physical Properties Of Solutions



# Review: Solution Terms & Types

- Solvent:** Larger portion of a solution
- Solute:** Smaller portion of a solution
- Solution:** A homogeneous mixture of two or more elements or compounds
- Solubility:** Measure of max amount of solute in solution

**TABLE 13.1**    **Types of Solutions**

Solute	Solvent	State of Resulting Solution	Examples
Gas	Gas	Gas	Air
Gas	Liquid	Liquid	Soda water (CO <sub>2</sub> in water)
Gas	Solid	Solid	H <sub>2</sub> gas in palladium
Liquid	Liquid	Liquid	Ethanol in water
Solid	Liquid	Liquid	NaCl in water
Solid	Solid	Solid	Brass (Cu/Zn), solder (Sn/Pb)

# More Solubility Terms

## Saturated solution:

Maximum amount of solute that stays in solution  
- Any additional solute will precipitate

## Unsaturated solution:

Contains less solute than in saturated solution

## Supersaturated solution:

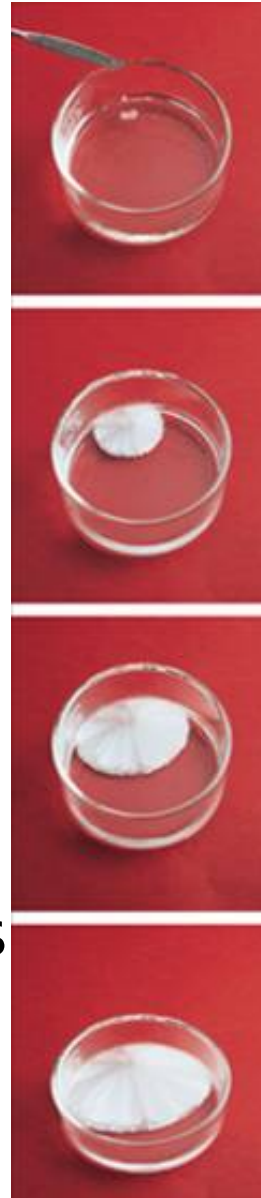
Contains more solute than in saturated solution  
- Extremely unstable (easy to make extra precipitate)

## Crystallization:

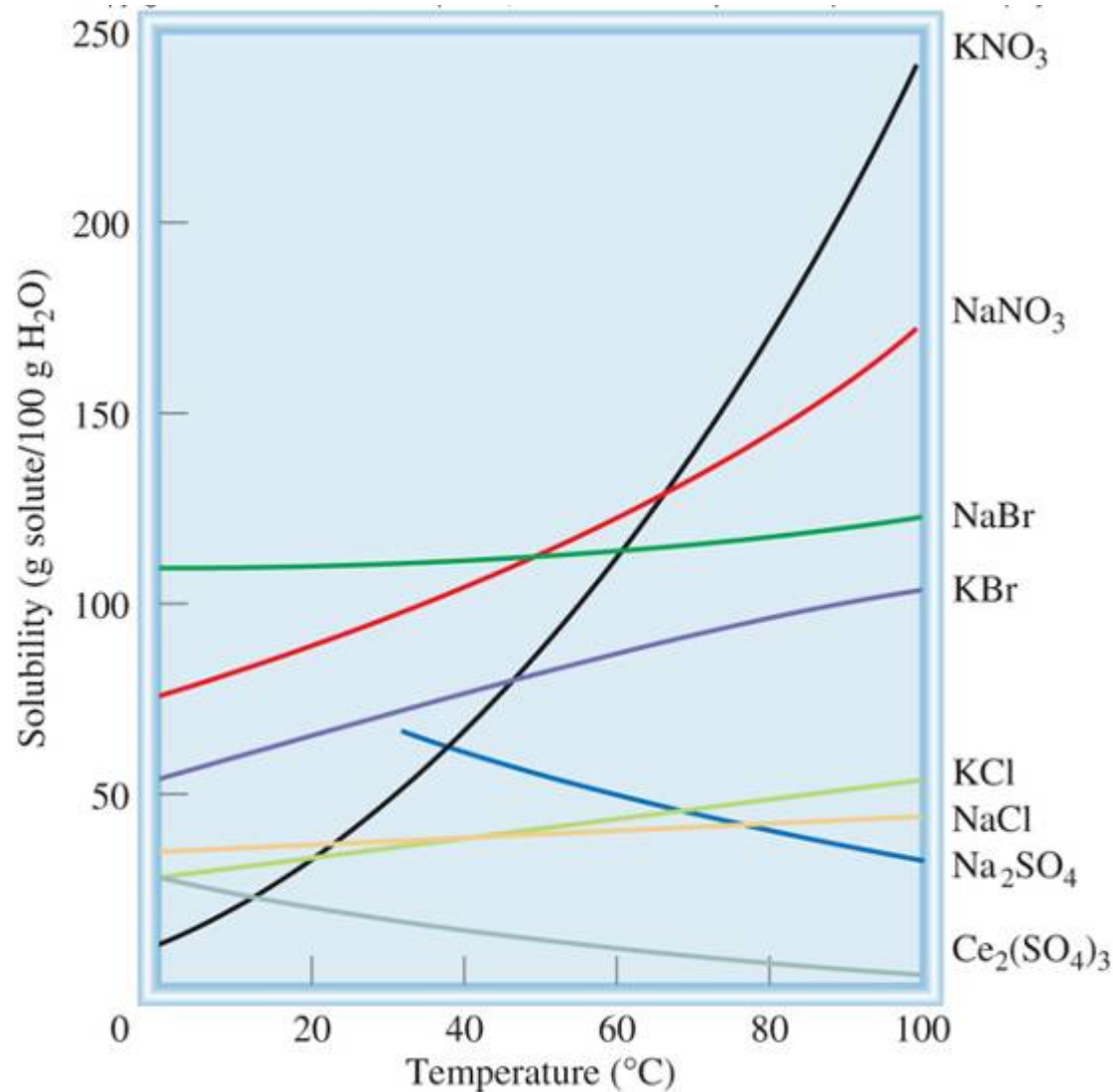
Extra solute in supersaturated solution precipitates & forms crystals

## Precipitation:

Solid comes out of solution, not always a crystal



# Solubility of Solids As A Function Of Temperature



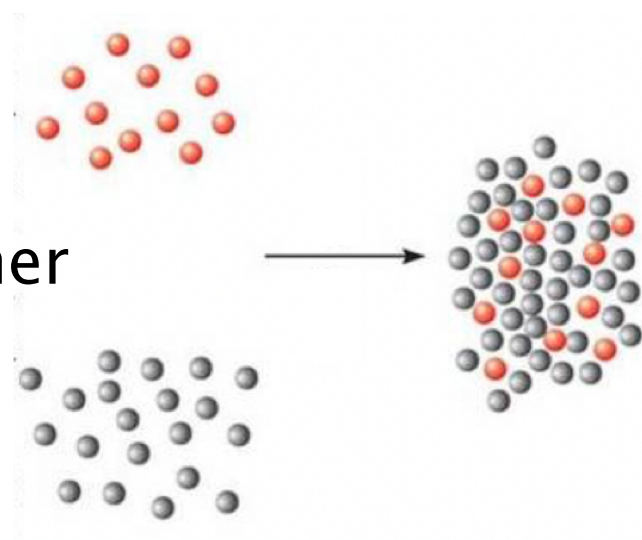
For most solids, as temp increases, solubility **increases**.

# Solvent/Solute Intermolecular Forces & Polarity<sup>5</sup>

**Rule of thumb is that "like dissolves like."**

Intermolecular forces are strongest for similar compounds

- Polar solvent/polar solute
- Nonpolar solvent/nonpolar solute
- Similar attractive forces lead to solvent and solute that are "miscible"
- **miscible** = fully dissolve in one another
  - resulting solution is stable



**Examples:**

- water/ethanol solutions
- Dissolution of ionic salts in  $\text{H}_2\text{O}$
- $\text{CCl}_4$  in benzene ( $\text{C}_6\text{H}_6$ )

# Concentration Units Review

$$\text{Molarity (M)} = \frac{\text{Moles Solute}}{\text{Liters of solution}} = \frac{\text{mol}}{\text{L}}$$

$$\text{Molality (m)} = \frac{\text{Moles Solute}}{\text{kg of solvent}} = \frac{\text{mol}}{\text{kg}}$$

Molarity is temperature dependent,  
Molality is NOT temperature dependent

$$\text{Percent by mass} = \frac{\text{Mass solute (g)}}{\text{Mass of solution (g)}} \times 100$$

Grams cancel so no units, just % sign

ppm = part per million (1 g/1x10<sup>6</sup>g)

7  
How many grams of sodium hydroxide are present in 0.500 kg of water if the solution concentration is 0.500 m?

**A: 10.0 g**

What mass of sodium hydroxide would be needed to make 4.00 L of a 0.300 m solution at 20°C?  
(density of water is 0.998 g/mL at 20°C)

**A: 47.9 g**



A 14.0% by mass acetic acid ( $\text{CH}_3\text{COOH}$ ) solution has a density of 1.02 g/mL. What is its molality?  
What is its molarity?

**Molality = 2.71 m**  
**Molarity = 2.38 M**

# The Solubilities Of Gases: Effect of Temperature

Gases are less soluble in liquids as temperature increases

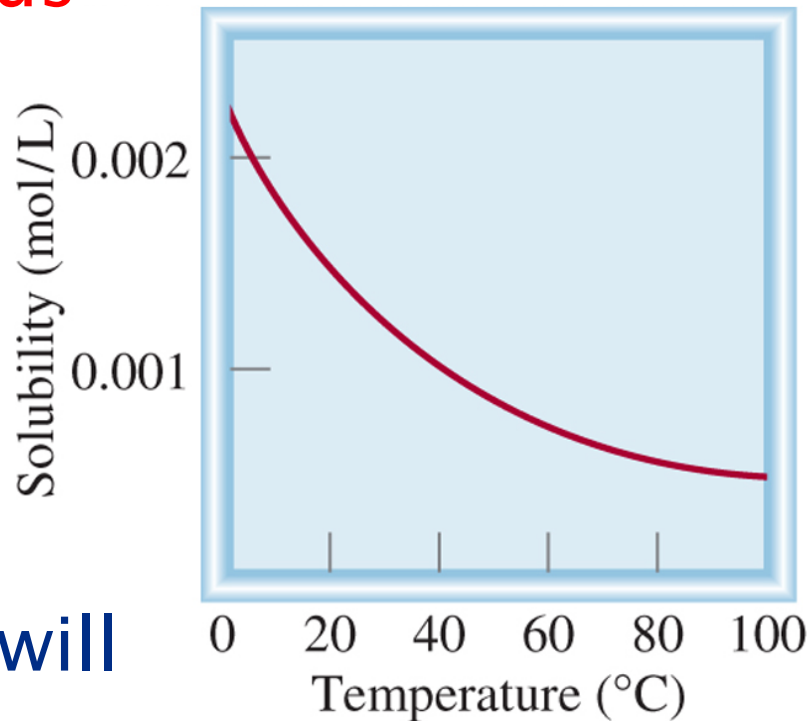
- Molecules move faster
- Disrupt intermolecular forces
- Gases escape the liquid
- Fewer gas molecules/atoms in liquid = Lower solubility

In sealed container, pressure will increase with increasing temp.

- More gas out of solution, moving faster, colliding more with container

Gas laws (Chapter 5!) govern gas phase and thus solubility

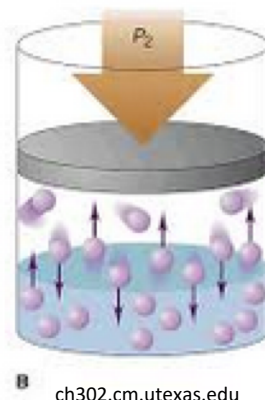
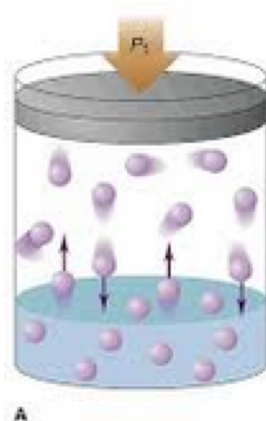
Solubility of O<sub>2</sub> in water



# The Solubilities Of Gases: Effect of Pressure

**Gas solubility in liquids increases as pressure increases**

- Molecules pushed too close together so they are forced back into liquid



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If pressure is decreased.....



**Henry's Law**  $c = kP$

$c$  = solubility or concentration

$P$  = pressure

$k$  = proportionality constant

Common units for  $k$ :  $c$  = moles/L and  $P$  = atm

If you know the concentration at one pressure,  $k$  allows you to determine concentrations at different pressures

# Vapor Pressures of Solutions

## Raoult's Law:

$$P_a = X_a P_a^\circ$$

$P_a$ : Vapor pressure of solvent “a” above a solution

$P_a^\circ$ : Vapor pressure of pure solvent “a”

$x_a$ : Mole fraction of “a” in the solution

$$x_i = \frac{\text{moles}_i}{\text{Moles}_{\text{total solution}}} = \frac{n_i}{n_{\text{total moles}}}$$

Works perfectly for ideal solutions

Works ok for the solvent in dilute solutions

- Solvent molecules in environment similar to pure solvent.

What is the vapor pressure of water in a 100.0g solution that contains 10.0g sucrose,  $C_{12}H_{22}O_{11}$  at  $40^{\circ}C$ ?  
The vapor pressure of pure water is 55.5 torr at  $40^{\circ}C$ .

MM: sucrose = 342.30 g/mol; water = 18.015 g/mol)

Step 1:Determine mole fraction of water

Step 2:Determine vapor pressure given  $P^{\circ} = 55.5$  torr at  $40^{\circ}C$

**A: 55.2 torr**

What mass (g) of ethanol (46.069 g/mol) must be added to 550.0 g water (18.015 g/mol) to give a solution with a vapor pressure 1.5 mmHg less than that of pure water at 30°C? Vapor pressure of water at 30°C is 31.8 mmHg.

**A: 69.6 g**

# Solutions Of Electrolytes

## Colligative properties:

- Physical properties of solutions that depend on the number of solute particles but NOT on the identity of the solute.
- Ex: Boiling Point, Freezing Point, Osmotic Pressure

## van't Hoff factor, $i$

- Used in solution equations for colligative properties (ex. Boiling point elevation:  $\Delta T_b = iK_b m$ )
- Nonelectrolytic solutions:  $i = 1$ .
- Electrolyte solutions:  $i$  = the number of ions the solute will dissociate into
- Ex: Hexane,  $i = 1$   
NaCl,  $i = 2$   
Pb(NO<sub>3</sub>)<sub>2</sub>,  $i = 3$

# Boiling Point Elevation

Vapor pressure above a solution is always less than vapor pressure above pure solvent.

1. Higher temperature needed for vapor pressure to hit 1 atm.
2. Boiling point of solution higher than boiling point of pure solvent
3. Boiling Point Elevation depends on:
  - Type of solvent
  - # of solute particles

$$\Delta T_b = iK_b m$$

$$T_b = T_b^\circ + \Delta T_b$$

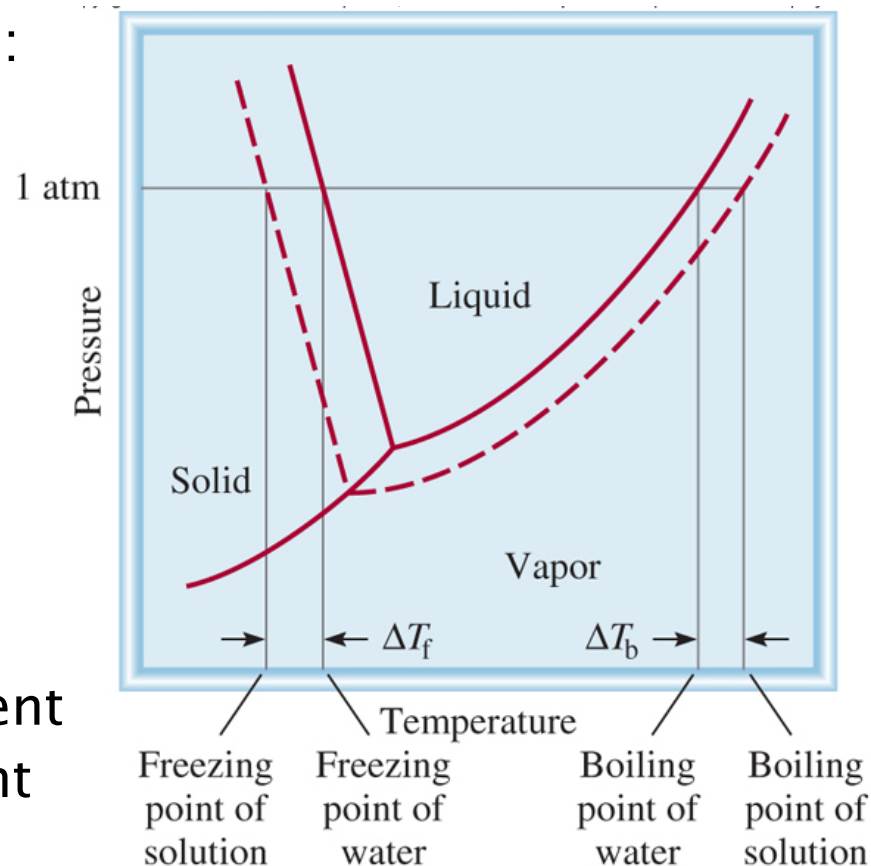
$m$  = solute molality

$T_b$  = boiling point of solution

$T_b^\circ$  = boiling point of pure solvent

$K_b$  = constant – based on solvent

$i$  = van't Hoff factor





# Freezing Point Depression

Solution freezes at lower temperature than pure solvent

Freezing Point Depression depends on

- Type of solvent
- # of solute particles

$$\Delta T_f = iK_f m$$

$$T_f = T_f^\circ - \Delta T_f$$

$m$  = solute molality

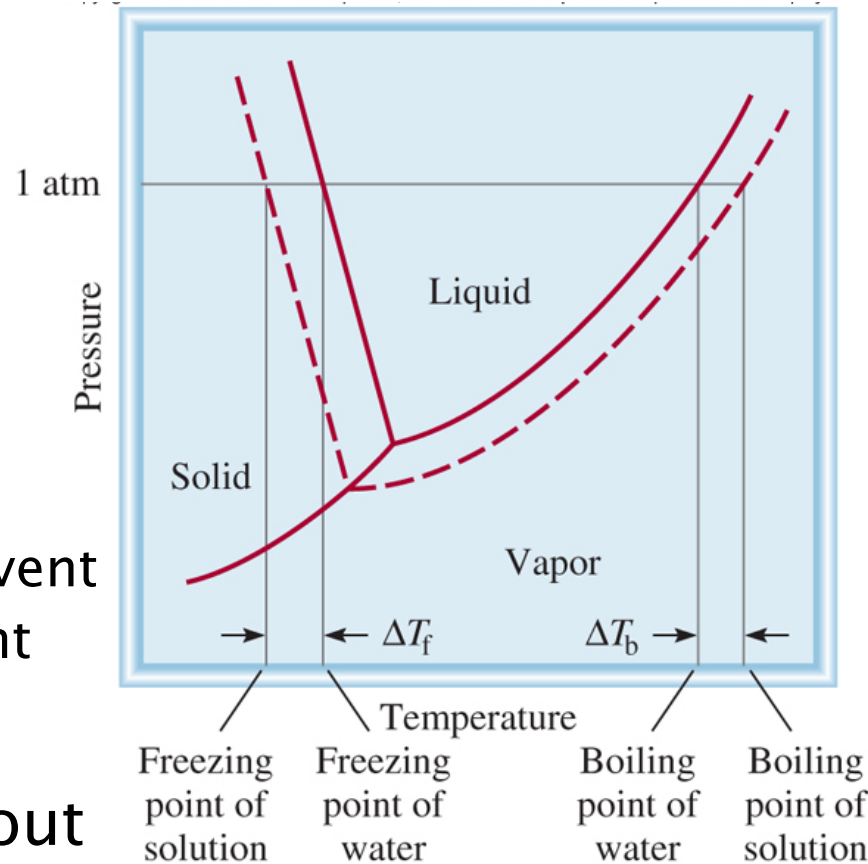
$T_f$  = freezing point of solution

$T_f^\circ$  = freezing point of pure solvent

$K_f$  = constant – based on solvent

$i$  = van't Hoff factor

- Only the pure solvent freezes out
- Pure substances: "sharp" melting point
- Impure materials: broad melting point range



What is the boiling point of a 0.886 m solution of pentane in benzene? For benzene: bpt =  $80.1^{\circ}\text{C}$ ,  $K_b = 2.53^{\circ}\text{C/m}$

A:  $82.3^{\circ}\text{C}$

What is the melting point of a 1.00 m solution of  $\text{CaCl}_2$  in water? For water: mpt =  $0.0^{\circ}\text{C}$ ,  $K_f = 1.86^{\circ}\text{C/m}$

A:  $-5.6^{\circ}\text{C}$

A solution of 2.366 g solute in 82.10 g cyclohexane freezes at 2.65°C. Determine the molar mass of the solute.

For cyclohexane,  $K_f = 20.0^\circ\text{C}/m$  and  $T_f^\circ = 6.55^\circ\text{C}$ .

Have freezing point of solution & pure solvent – can use  $\Delta T_f = iK_fm$  to determine the **molality** of the solution

Use mass of solvent & molality to calculate moles solute

Given mass solute, so can calculate molar mass of solute

A: 148 g/mol

# Constants

Will be provided on exams if needed

**TABLE 13.2**

**Molal Boiling-Point Elevation and Freezing-Point Depression Constants of Several Common Liquids**

Solvent	Normal Freezing Point (°C)*	$K_f$ (°C/ <i>m</i> )	Normal Boiling Point (°C)*	$K_b$ (°C/ <i>m</i> )
Water	0	1.86	100	0.52
Benzene	5.5	5.12	80.1	2.53
Ethanol	−117.3	1.99	78.4	1.22
Acetic acid	16.6	3.90	117.9	2.93
Cyclohexane	6.6	20.0	80.7	2.79

# Osmotic Pressure

**Semi-permeable membranes:** Materials with tiny pores that only allow solvent molecules to pass

- solute cannot get through the membrane

**Osmosis:** Net flow of solvent molecules through a semi-permeable membrane from dilute to concentrated solution.

**Osmotic Pressure ( $\pi$ ):** Pressure needed to stop osmotic flow

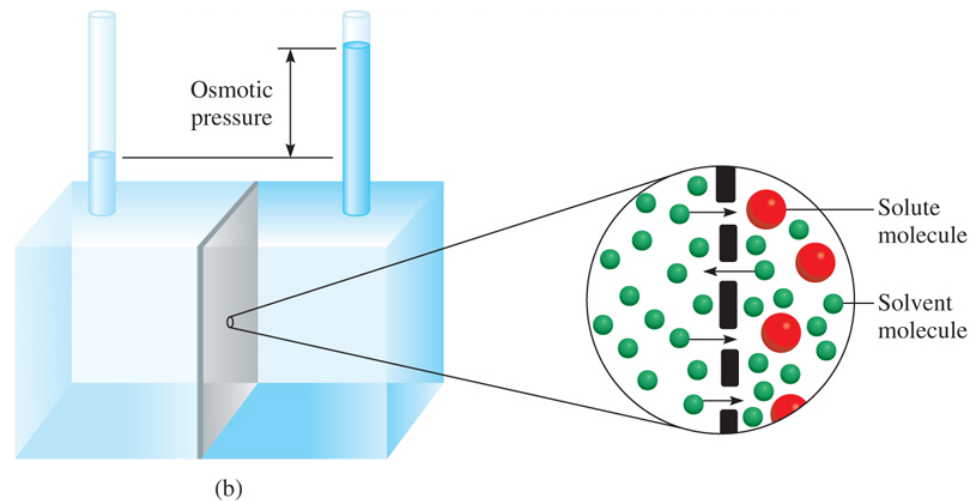
- $\pi$  depends on:
  - concentration
  - temperature

$$\pi = iMRT$$

M= molarity

R= gas constant  $\left(0.0821 \frac{\text{L atm}}{\text{mol K}}\right)$

T= temperature



What is the osmotic pressure of a 0.238 M aqueous sugar solution at 25°C?

A: 5.83 atm

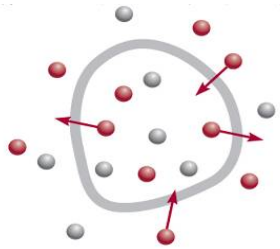
What is the molar mass of a solute if 397.2 g of the compound dissolved in water produces 592.4 mL of a solution that has an osmotic pressure of 1.98 atm at 35°C?

A: 8570 g/mol

# Practical Applications Of Osmosis

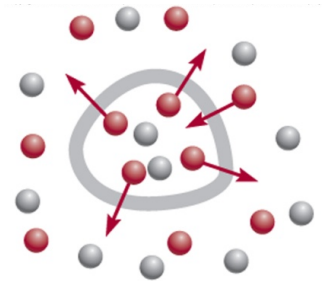
## Isotonic Solution: Organ Transplants

- Same concentration on both sides of membrane
- Organs would burst if stored in water



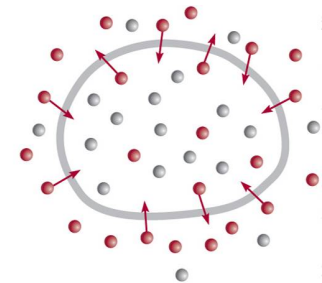
## Hypertonic Solution: Food Preservation

- Higher concentration outside the membrane
- Salt pulls water from microbes and kills them



## Hypotonic Solution: Tree Growth

- Lower concentration outside the membrane
- Water pulled through sap to top of trees



## Reverse osmosis: Water Purification

- Reversing the net flow of solvent through a membrane by applying pressure greater than osmotic pressure.
- Obtain water with low solute concentration