

Chemistry 431
Exam Number 3
Fall 2023
50 Minutes
Solutions

$$R = 8.3144 \text{ J mol}^{-1} \text{ K}^{-1}$$

$$R = .08314 \text{ L bar mol}^{-1} \text{ K}^{-1}$$

$$k = 1.381 \times 10^{-23} \text{ J molecule}^{-1} \text{ K}^{-1}$$

$$h = 6.626 \times 10^{-34} \text{ Js}$$

$$N_A = 6.022 \times 10^{23} \text{ molecules mol}^{-1}$$

$$1 \text{ kg} = 1000. \text{ g}$$

$$1 \text{ L} = 10^3 \text{ cm}^3$$

$$10^2 \text{ cm} = 1 \text{ m}$$

$$T = t + 273.15$$

$$0.001 \text{ m}^3 \text{ L}^{-1}$$

Name:

1. Show that for any substance

$$\left(\frac{\partial U}{\partial S}\right)_P = T - \frac{PT\left(\frac{\partial V}{\partial T}\right)_P}{C_P}$$

where C_P is the constant pressure heat capacity of the substance. (33 Points)

Answer:

$$dU = TdS - PdV$$

$$\left(\frac{\partial U}{\partial S}\right)_P = T - P\left(\frac{\partial V}{\partial S}\right)_P$$

$$dH = TdS + VdP \quad \left(\frac{\partial V}{\partial S}\right)_P = \left(\frac{\partial T}{\partial P}\right)_S$$

$$\left(\frac{\partial U}{\partial S}\right)_P = T - P\left(\frac{\partial T}{\partial P}\right)_S$$

$$\left(\frac{\partial T}{\partial P}\right)_S \left(\frac{\partial P}{\partial S}\right)_T \left(\frac{\partial S}{\partial T}\right)_P = -1$$

$$\left(\frac{\partial T}{\partial P}\right)_S = -\frac{\left(\frac{\partial S}{\partial P}\right)_T}{\left(\frac{\partial S}{\partial T}\right)_P}$$

$$dG = -SdT + VdP \quad \left(\frac{\partial S}{\partial P}\right)_T = -\left(\frac{\partial V}{\partial T}\right)_P$$

$$dS = \frac{1}{T}dH - \frac{V}{T}dP \quad \left(\frac{\partial S}{\partial T}\right)_P = \frac{C_P}{T}$$

$$\left(\frac{\partial T}{\partial P}\right)_S = \frac{T\left(\frac{\partial V}{\partial T}\right)_P}{C_P}$$

$$\left(\frac{\partial U}{\partial S}\right)_P = T - \frac{PT\left(\frac{\partial V}{\partial T}\right)_P}{C_P}$$

Name:

2. As a function of temperature and pressure, ice takes on many different crystal structures named I_h , I_2 , I_3 , and so on. Ice I_h , called *hexagonal ice*, is the most stable crystal structure of the system near 273 K and a pressure of 1 bar. At a pressure of 2.13×10^3 bar and a temperature of 238 K, crystal structures I_h and I_2 are in equilibrium with each other. Given $\Delta_{r,m}H^\ominus = -752.4 \text{ J mol}^{-1}$ for the process



is independent of temperature and pressure, and given the density of I_h ice and I_2 ice are respectively $\rho_h = 921 \text{ g L}^{-1}$ and $\rho_2 = 1170 \text{ g L}^{-1}$, calculate $\Delta_{r,m}G^\ominus$ for process (1) at 273 K. (33 Points)

Answer:

$$\begin{aligned} \Delta_{r,m}G(T_2, P) - \Delta_{r,m}G^\ominus(T_2) &= \Delta_{r,m}V(P - P^\ominus) \\ \frac{\Delta_{r,m}G^\ominus(T_2)}{T_2} - \frac{\Delta_{r,m}G^\ominus(T_1)}{T_1} &= \Delta_{r,m}H^\ominus \left(\frac{1}{T_2} - \frac{1}{T_1} \right) \end{aligned}$$

Combining

$$\begin{aligned} \frac{\Delta_{r,m}G(T_2, P)}{T_2} - \frac{\Delta_{r,m}G^\ominus}{T_1} - \frac{\Delta_{r,m}V(P - P^\ominus)}{T_1} &= \Delta_{r,m}H \left(\frac{1}{T_2} - \frac{1}{T_1} \right) \\ \frac{\Delta_{r,m}G(T_2, P)}{T_2} &= 0 \end{aligned}$$

at equilibrium. Then

$$\begin{aligned} \Delta_{r,m}G^\ominus(273) &= -\Delta_{r,m}V(P - P^\ominus) - \Delta_{r,m}H \left(\frac{T_1}{T_2} - 1 \right) \\ &= - \left(\frac{\text{L}}{1170 \text{ g}} - \frac{\text{L}}{921 \text{ g}} \right) \left(\frac{18.0 \text{ g}}{\text{mol}} \right) (2130 \text{ bar} - 1 \text{ bar}) \left(\frac{100 \text{ J}}{\text{L bar}} \right) = 996 \text{ J mol}^{-1} \end{aligned}$$

Name:

3. The equilibrium degree of dissociation of gas-phase bromine pentafluoride according to the reaction



at a total pressure of $P_{tot} = 3.00$ bar is $\alpha_{1000} = 0.121$ at 1000. K and $\alpha_{1100} = 0.278$ at 1100. K. Assuming $\Delta_{r,m}H^\ominus$ to be temperature independent, calculate the standard entropy change for the reaction at 1500. K. (34 Points)

Answer:

Let n_0 = the initial number of moles of $\text{BrF}_{5(g)}$

	n_{BrF_5}	n_{BrF_3}	n_{F_2}
initial	n_0	0	0
change	$-\alpha n_0$	αn_0	αn_0
equilibrium	$n_0(1 - \alpha)$	αn_0	αn_0

$$n_{total} = 2\alpha n_0 + (1 - \alpha)n_0 = (1 + \alpha)n_0$$

$$K_P = \frac{\frac{P_{\text{BrF}_3}}{P^\ominus} \frac{P_{\text{F}_2}}{P^\ominus}}{\frac{P_{\text{BrF}_5}}{P^\ominus}} = \frac{\left(\frac{\alpha}{1 + \alpha} \frac{P}{P^\ominus}\right)^2}{\frac{1 - \alpha}{1 + \alpha} \frac{P}{P^\ominus}} = \frac{\alpha^2}{1 - \alpha^2} \frac{P}{P^\ominus}$$

$$K_P(1000) = 4.46 \times 10^{-2} \quad K_P(1100) = 2.51 \times 10^{-1}$$

$$\ln \frac{K_P(T_2)}{K_P(T_1)} = \frac{\Delta_{r,m}H^\ominus}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right)$$

$$\ln \frac{0.251}{0.0446} = \frac{\Delta_{r,m}H^\ominus}{R} \left(\frac{1}{1000 \text{ K}} - \frac{1}{1100 \text{ K}} \right) \quad \frac{\Delta_{r,m}H^\ominus}{R} = 19000 \text{ K}$$

$$\ln \frac{K_P(1500)}{0.0446} = 19000 \text{ K} \left(\frac{1}{1000 \text{ K}} - \frac{1}{1500 \text{ K}} \right) \quad K_P(1500) = 25.3$$

$$\Delta_{r,m}H^\ominus = (19000 \text{ K})(8.3144 \text{ J mol}^{-1}\text{K}^{-1}) = 158000 \text{ J mol}^{-1}$$

$$\Delta_{r,m}G^\ominus = -RT \ln K_P = -(8.3144 \text{ J mol}^{-1}\text{K}^{-1})(1500 \text{ K}) \ln(25.3) = -40240 \text{ J mol}^{-1}$$

$$\Delta_{r,m}S^\ominus = \frac{\Delta_{r,m}H^\ominus - \Delta_{r,m}G^\ominus}{T}$$

$$= \frac{158000 \text{ J mol}^{-1} - (-40240 \text{ J mol}^{-1})}{1500 \text{ K}} = 132 \text{ J mol}^{-1}\text{K}^{-1}$$

Name:

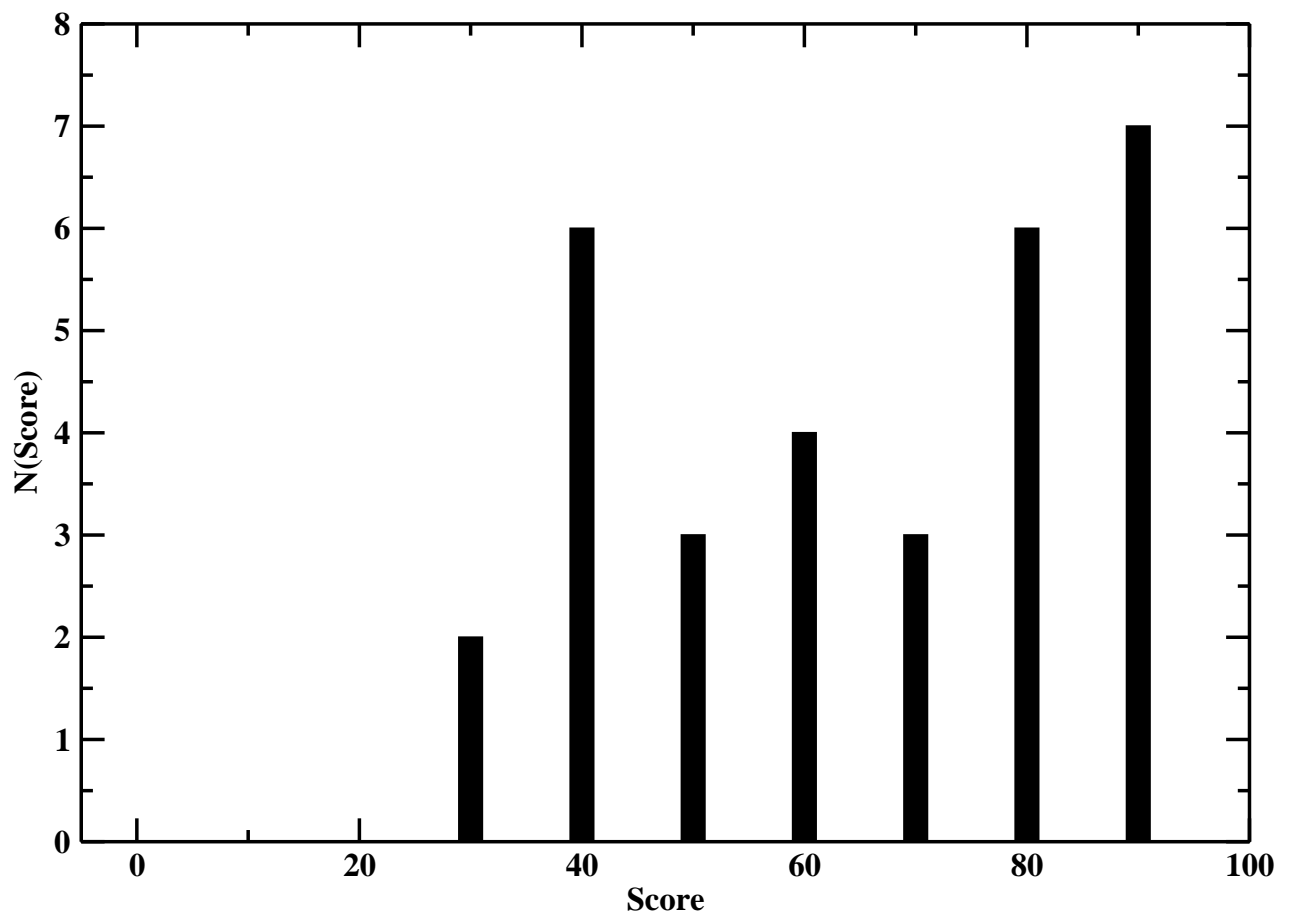


Figure 1: **High** = 100, **Median** = 72, **Mean** = 70